DETERMINATION OF ERRORS

INA

SERIES TRANSFORMER

BY

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Armour Institute of Technology



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Determination of errors in a

series transformer

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DETERMINATION OF ERRORS

IN A

SERIES TRANSFORMER

A THESIS

PRESENTED BY

E. M. BEATY

V. F. VACEK

TO THE

PRESIDENT AND FACULTY

OF

ARMOUR INSTITUTE OF TECHNOLOGY

FOR THE DEGREE OF

BACHELOR OF SCIENCE IN ELECTRICAL ENGINEERING

HAVING COMPLETED THE PRESCRIBED COURSE OF STUDY IN

ELECTRICAL ENGINEERING

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Albert A. Smithe.

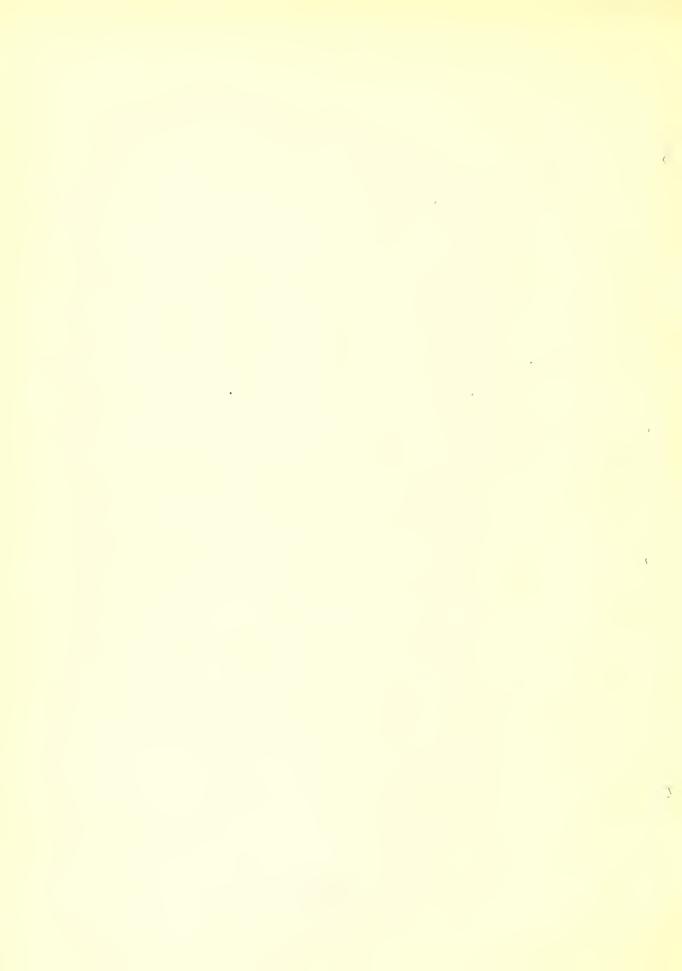
A. M. Harry



It was intended at the outset to run a test on several transformers of various types, but it was later found that the subject
took a great deal more time than was anticipated. For this reason
a full set of data was obtained on only one transformer.

The calculated data and the curves shown in this thesis are those for a General Electric Series Transformer, Type S, Form D, #30286; built for 13500 volts on the mains. Natio 20 to 1. Full load 75 amperes, thirty minute load 100 amperes.

Further data on a 25 ampers transcenser is included in this thesis but it is not worked an.



A series transformer is a device commonly used in high potential power lines for supplying current to an ammeter or the series coil of a wattmeter.

It being undesirable to bring the high potential feeders directly to the switch board on account of the danger thus involved the series transformer was developed.

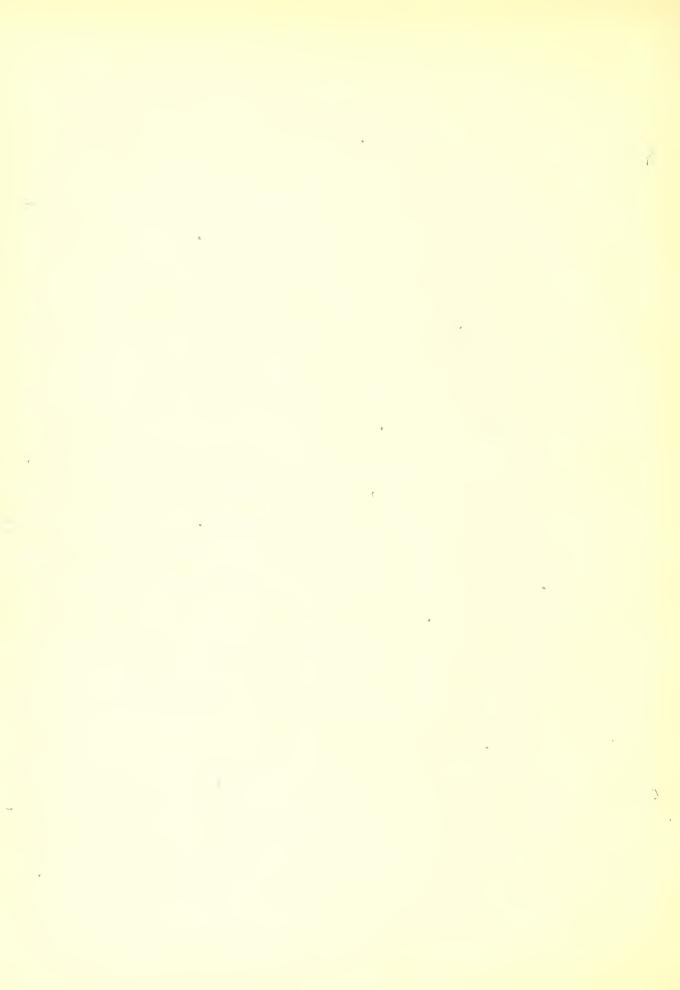
It occupies the same place in alternating current work as does the shunt in direct current lines, namely; that of supplying a definite ration of the total current flowing through the lines to instruments whose scales are so calibrated that the total amount of current flowing is read, instead, of just that portion which flows through them.

The transformer is essentially a few turns of heavy wire, are wound on a porcelain core, which is connected in series with the line, in which the current is to be measured. The secondary consists of a large number of smaller turns wound around the primary winding. The measuring instruments connect directly to these secondary terminals.

If the transformer is designed for some particular instrument with its known length of leads from the transformer to the switch board it can be so constructed that the percent error on all loads is very small.

As the above is very seldom the case, since certain types of transformers are used on different types of instruments and different lengths of leads, an error is introduced which depends upon the nature of the secondary circuit and the size of the load.

The commonly recognized error of these transformers is that of variation of the ratio of transformation. Another source of



error, which is seldom mentioned is that of the phase relations of the currents in the primary and secondary of the transformer. The error caused by this latter is practically neglegible at unity power factor but rapidly increases for lower power factors.

In a transformer the primary and secondary currents are nearly always assumed to be 180° apart. This is very seldom the case but does not make much difference in general cases.

In a series transformer where its sole function is to supply current for power measuring instruments an error, however small, causes a loss where large amounts of power are measured.

The current in the secondary of a transformer of the series

type instead of being just 180° behind the current in the primary,

(the 180° position)

lags it by a small angle which will be called alpha (a) in this

work.

The object of the following work is to find the value of that angle and also the ratio of transformation under different characters of secondary circuits for loads varying from light loads to over loads. The value of the ratio of transformation is a very easy quantity to obtain since it is just the ratio of the primary to the secondary current and these values can be obtained very readily. The method of obtaining the phase angle was a harder matter as the literature on that subject was of very meagre nature. The only reference found was that in the transactions of the American Institute of Electrical Engineers of 1906.

An oscillograph was thought of, but as the angle to be measured was so small compared to the scale of the oscillograms which could be obtained that another method was thought more applicable.

The method used is a rather simple one and consists of two sensitive dynamometers, the stationary coils of which are connected in parallel, one of them first going through an ammeter.

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These coils are then connected through a bank of lamps to the secondary of a three phase, squirrle cage, induction motor, the secondaries of each phase being open and connected to sliprings. By supplying current to the primary of the induction motor a revolving field is set up and by moving the rotor the desired amount and clamping it in place, a current which varies from the primary current by an amount equal to from zero to 120, depending upon the position of rotor, can be obtained.

The moving coil of one dynamometer was connected to a shunt in the primary circuit. The moving coil of the other dynamometer was connected through an ammeter to the secondary of the transformer to be tested. A double pole switch was placed in each circuit so that the instruments could be cut out when desired. A single pole switch was placed across the secondary terminals of the transformer so it could be shortened when the other switches were open. This was necessary because if it was left open a high e.m.f. would be set up in the secondary due to the primary current. This e.m.f. would be liable to puncture the insulation.

As a large current was needed the most convenient way of obtaining it was decided to be that, of using a high current transformer which had a ratio of eleven, twenty-two, forty-four, depending upon the way of connecting. A current as high as three thousand amperes could be obtained with this if desired but as only one hundred was needed it was connected up with the twenty-two ratio and by varing the current in the primary by means of a lamp rack and some carbon rheostats the value of the secondary current of this transformer could be changed at will.

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The secondary of this transformer was connected directly through the primary of the series transformer and the shunt spoken of before.

A frequency meter was also supplied, as were double-throw switches for balancing the dynamometers against each other if desired. The scheme of wiring can easily be seen from the accompaning blue print.

The method of working the apparatus is as follows:

Current is sent through both coils of the dynamometer by manipulation of the lamp racks. Then by moving the handle connected to the rotor of the induction motor the phase relation of the current in the stationary coils is adjusted to 90° difference from that in the moving coil of the dynamometer connected onto the shunt. The current in the coil connected to the shunt is in phase with the primary current of the transformer. A 90° difference in phase relation of the currents will cause the dynamometer connected to the shunt to read zero.

If the current in the secondary of the transformer is just 180° out of phase with the primary current the dynamometer across it will read zero. If it does not read zero, the deflection is noted and the values of the currents in each of its coils are taken. The deflection obtained is proportional to the sine of the angle of lag since the deflection of the dynamometer is equal to the products of the currents through each coil times the cosine of the angle ketween them or D=KII, cos e. By adjusting the dynamometer across the shunt for zero deflection e becomes 90° so the angle between the currents in the second dynamometer is (90°-a). Therefor D=KII, cos(90°-a)=KII, sin(a).

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The dynamometer was calibrated as an ammeter on direct current so the value of the cosine is one and as the two coils were in series I.I. then D=KI. This enabled one to determine the value of K for different deflections and a curve was plotted so these values could be taken off. The ammeters were calibrated and curves plotted for them as was also done for all the instruments used.

When the experiment first started an ammeter was placed in the circuit of the moving coil connected across the shunt so by ratio of the resistance of these two circuits and the reading of the ammeter in the secondary of the transformer the ratio of transformation could be obtained directly. This cut down the sensibility of the dynamometer so much that it was taken out and the ratio obtained separately by means of a hot wire ammeter connected across the shunt. By plotting a curve for these ratio readings the value of the primary current corresponding to the secondary current taken during the phase angle readings could be obtained and the ratio obtained by their division.

In order to obtain the impedance of the secondary circuit a special instrument had to be used because there was no low reading alternating current voltmeter obtainable. In order to obtain an instrument, a Whitney hot wire ammeter which is commonly used across a shunt was calibrated as a voltmeter as follows:

It was placed across the shunt and readings taken of current flowing through the shunt and the reading of ammeter. A millivoltmeter was then placed across the shunt and readings of it taken corresponding to line current. By plotting a curve against ammeter readings and millivolt readings the calibration of the ammeter as a voltmeter was obtained.

-• τ :

In obtaining the impedance drops, the drop had to be taken over the ammeter which was in the circuit or the true value of current flowing through the circuit could not be obtained. As this could not always be done it was necessary to calibrate the instrument as an ammeter without its shunt. Then by subtracting the current flowing through it from the ammeter reading the true value of the current in the circuit was obtained and then $Z = \frac{E}{I}$ where E is the voltage as indicated by the instrument and I is the corrected current. This was necessary because the instrument had such a low resistance that more current flowed through it, than did through the circuit to be measured. The resistance of the circuit was obtained by the fall of potential method using a calibrated ammeter and voltmeter.



The symbols and letters used in this work have the following meanings:

R. : Resistance of secondary circuit.

L = Reactance of secondary circuit.

Iph : Current in phase-shifter.

Is: Current in transformer secondary.

Ip : Current in transformer primary.

Defl.: Dynamometer deflection.

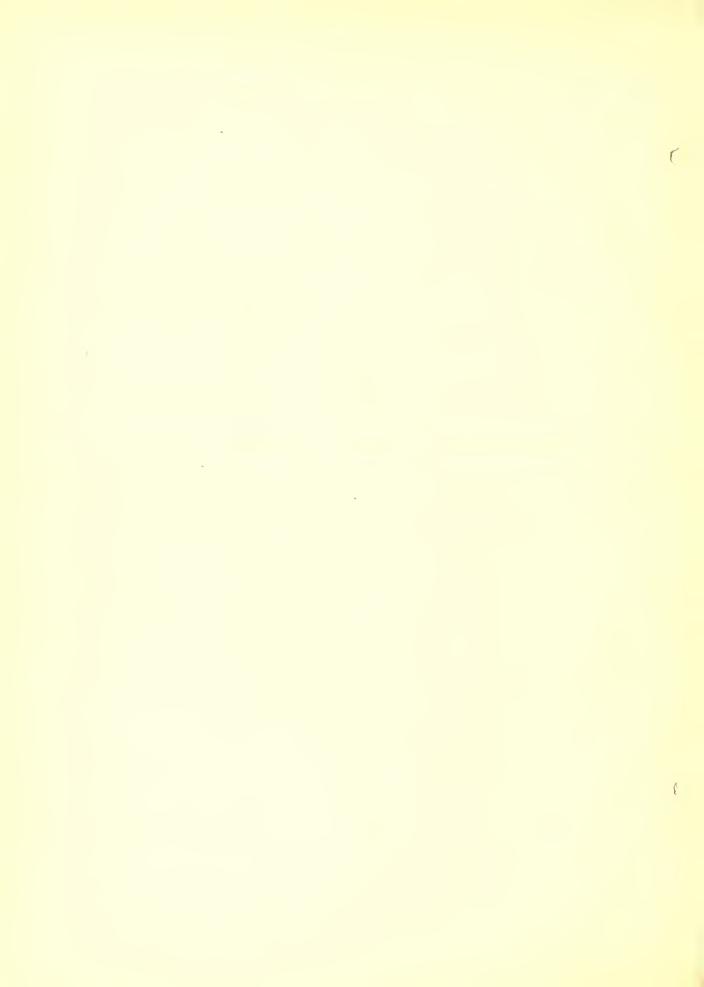
K = Dynamometer constant.

R = Ratio of primary current to secondary current.

= Corrected values of above symbols.

The circuits used are composed of the following; as taken from the data sheets on resistance and impedance.

No.	Character.
3	(b)+(c)
4	(a) + (c)
5	(c)+(h)
6	(c) + (i)
7	(e)
8	(f)
10	(g)
11	(k)+(c)



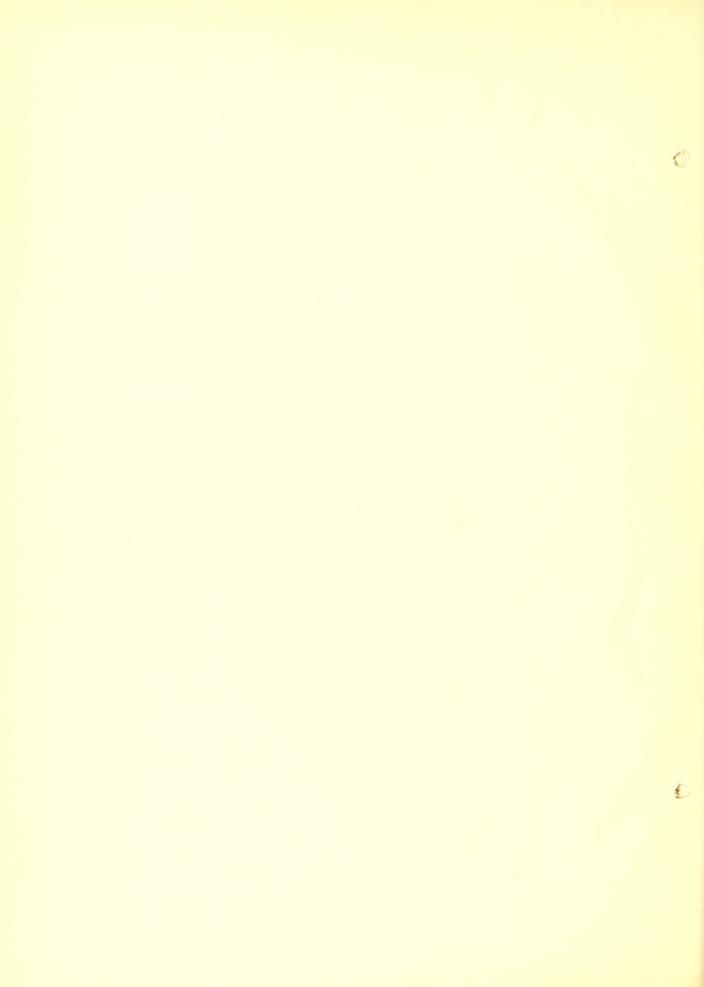
The nature of the secondary circuits used are as follows:

No.	. R	\mathbf{L}
4 5 11 13 6	.35460	.0035860 .0058000 .0096260 .0166000
1 7 12 8 10	.09060 .12870 .21200 .22920 .25900	.0003460
3	.22060	.0010740

n . A





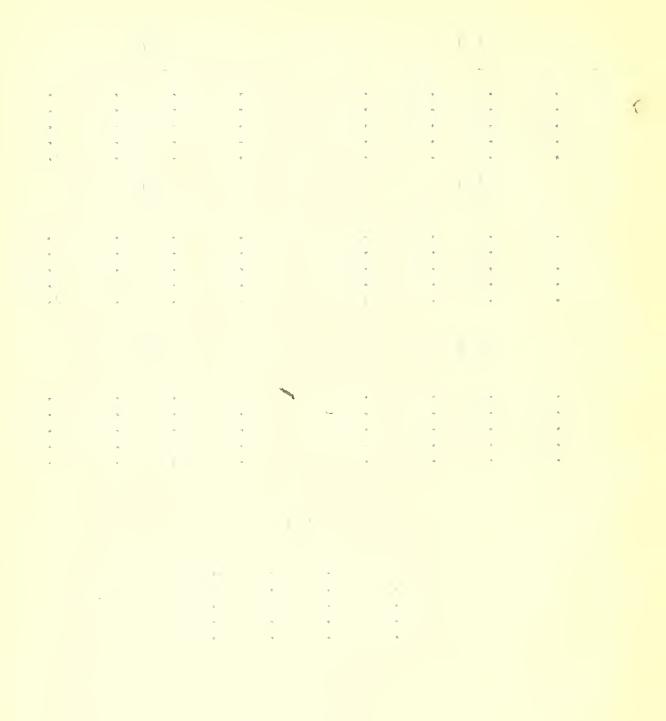


		(a)		Resistan	ce.		(b)		
I 1 2 3 4 5	E 0:270 0:530 0:795 1:050 1.300	#I 0.99 1.98 2.96 3.89 4.86	#E 0.260 0.520 0.790 1.035 1.270	R 0'.263 0'.263 0'.267 0.266 0.262	I 1 2 3 4 5	E 0'.135 0'.265 0'.392 0'.520 0.640	#I 0.99 1.98 2.96 3.89 4.86	#E 0.130 0.265 0.380 0.510 0.625	R 0.1315 0.1337 0.1285 0.1278 0.1286
I	E	(c) #I	#E	R	I	E	(d) #I	#E	R
1 2 3 4 5	0.090 0/180 0.275 0.368 0.455	0.99 1.98 2.96 3.89 4.86	0.090 0.175 0.270 0.360 0.445	0.0910 0.0885 0.0913 0.0903 0.0917	1 2 3 4 5	0'.105 0'.210 0'.230 0'.425 0.525	0.99 1.98 2.96 3.89 4.86	0.105 0.205 0.310 0.415 0.510	0.1062 0.1035 0.1047 0.1040 0.1050
I	E	(e) #I	#E	, R	I	E	(f) #I	<i>, #</i> E	R
1 2 3 4 5	0.238 0.465 0.690 0.920 1/135	0.99 1.98 2.96 3.89 4.86	0.237 0.455 0.670 0.900 1.100	0.2495 0.2300 0.2265 0.2310 0.2290	1 2 3 4 5	0.132 0.258 0.392 0.513 0.640	0.99 1.98 2.96 3.89 4.86	0.130 0.250 0.380 0.500 0.625	0.1315 0.1265 0.1285 0.1285 0.1285

7)

1)

	(g)						
I	E	#1	#E	R			
1	0.262	0.99	0.26	0,263			
2	0.520	1.98	0.51	0.257			
3	0.775	2:.96	0.76	0.257			
4	1.035	3.89	1.01	04.260			
5	1.283	4.85	1.25	0.257			



Impedance.

(a)

I ₂ 1.423 2'.152 2'.808 5'.150 3.478	E' _H 40'.0 60'.0 80'.0 90.0 100.0	Alt. 50/50	#I2 1.430 2.165 2.830 3.185 3.525	7 I ни 1.245 1.860 2.440 2.750 3.000	0'185 0'305 0'390 0'455 0.525	E 0.117 0.171 0.229 0.257 0.286	Z 0.633 0.562 0.588 0.565 0.545
1.890 2.800 3.738 4.600	E m 40.0 60.0 80.0 100.0	Alt. 50.50	#I2 1.915 2.825 3.785 4.65	I _{NW} 1.245 1.860 2.440 3.000	I ₂ 0.670 0.965 1.345 1.650	E 0.117 0.171 0.229 0.286	Z 0.1750 0.1775 0.1700 0.1735
			(c)				
1. 0.550 1.085 1.600 2.148 2.375 2.650 1.075 1.600 2.185 2.435 2.718	E _H 20.0 40.0 60.0 80.0 90.0 100.0 40.0 60.0 90.0	Alt. 50.50 "" "" "" "" "" "" "" "" "" "" "" "" ""	#I. 0.530 1.085 1.600 2.165 2.405 2.675 1.075 1.610 2.225 2.470 2.750	I H.W O O O O O O O O O O O O O O O O O O O	I. 0.530 1.085 1.600 2.165 2.405 2.675 1.075 1.610 2.225 2.470 2.750	E 0.064 0.117 0.171 0.229 0.257 0.286 0.117 0.171 0.229 0.257 0.286	Z 0.121 0.108 0.107 0.106 0.1068 0.107 0.1088 0.106 0.103 0.104 0.104

Impedance.

(d)

0'.875 1'.335 1.818 2.028 2.26	40.0 60.0 80.0 90'.0	Alt. 51.0	#I2 0.875 1.339 1.835 2.040 2.290	I н.w O O O O	7. 0.875 1.339 1.835 2.040 2.290	E 0.117 0.171 0.229 0.257 0.286	Z 0.1340 0.1275 0.1250 0.1400 0.1250
			(h)				
1.345 1.960 2.550 3.165	E # 40.0 60/0 80/0 100.0	Alt. 50.50	# I ₂ 1.345 1.980 2.556 3.200	Iv 1.245 1.860 2.440 3.000	T. 0.100 0.120 0.110 0.200	E 0.117 0.171 0.329 0.286	Z 1.170 1.425 2.80 1.430
			(i)				
1.275 1.275 1.870 2.445 3.030	E _A 24.0 40.0 60.0 80.0	Alt. 50.25	#I ₂ 0'.780 1.275 1.900 2.460 3.060	I,w 0.760 1.245 1.860 2.440 3.000	1. 0.02 0.030 0.04 0.020 0.060	E 0.076 0.117 0.171 0.229 0.286	Z 3.80 3.90 4.50 1.44 4.75
			(k)				
I, 1.380 2.050 2L695 3.310	E _H 40'.0 60.0 80'.0	Alt. 50.50	#I2 1.370 2.060 2.710 3.350	I	I. 0'.115 0.200 0'.270 0.350	E 0.117 0.171 0.229 0.286	Z 1.017 0.850 0.850 0.820

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Ratio Readings.

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I,	Ιρ	Is	Ι _Η	I,	\mathbf{I}_{P}	I_s
0.50	11.5	0.50	12.0	0.60	15.5	0.60
						1.21
	-					1.64
			_		-	2.10
	-				-	2.55
_	-	_		-	-	3.13
_	_			-	-	3.73
-					-	4.20
						4.70
4.98	97.8	4.98	95.2	4.97	96.5	4.98
	I,	I, I, 0'.50 11'.5 1.13 22.8 1.63 32.5 2.08 41.0 2.56 51'.0 3.07 61'.2 3'.63 71.8 4.10 82.0 4'.60 91'.3	I. I, Is 0.50 11.5 0.50 1.13 22.8 1.13 1.63 32.5 1.65 2.08 41.0 2.10 2.56 51.0 2.56 3.07 61.2 3.11 3.63 71.8 3.68 4.10 82.0 4.15 4.60 91.3 4.65	I. I. I. 0'.50 11'.5 0.50 12.0 1.13 22.8 1.13 22.0 1'.63 32.5 1.65 32.0 2.08 41.0 2.10 40.0 2.56 51'.0 2.56 50.0 3.07 61'.2 3.11 60'.0 3'.63 71.8 3'.68 70.0 4.10 82'.0 4.15 80'.0 4'.60 91'.3 4.65 90'.0	I. I. I. I. 0.50 11.5 0.50 12.0 0.60 1.13 22.8 1.13 22.0 1.21 1.63 32.5 1.65 32.0 1.62 2.08 41.0 2.10 40.0 2.08 2.56 51.0 2.56 50.0 2.55 3.07 61.2 3.11 60.0 3.09 3'.63 71.8 3'.68 70.0 3.68 4.10 82.0 4.15 80'.0 4.14 4'.60 91'.3 4.65 90'.0 4'.65	I, I, I, I, I, 0.50 11.5 0.50 12.0 0.60 15.5 1.13 22.8 1.13 22.0 1.21 24.5 1.63 32.5 1.65 32.0 1.62 33.5 2.08 41.0 2.10 40.0 2.08 41.0 2.56 51.0 2.56 50.0 2.55 51.0 3.07 61.2 3.11 60.0 3.09 61.2 3.63 71.8 3.68 70.0 3.68 71.8 4.10 82.0 4.15 80.0 4.14 82.0 4.60 91.3 4.65 90.0 4.65 91.3

Circuit #4

$I_{.H}$,I ₂	Ip.	,I _s
10.0	0.58	13.5	0.58
22.0	1,20	24.5	1.21
30.0	1,55	31.7	1.56
40.0	2.08	41:0	2.09
50.0	2.55	51.0	2.61
60.0	3.09	61.2	3,13
70.0	3,65	71.8	3.70
80.0	4.11	82.0	4.16
90.0	4.63	91.3	4.68
95.0	4.95	96.2	4.97

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		Ra	atio Read	dings.			
	Circuit				Circuit	#6	
$\mathbf{I}_{\mathcal{H}}$	I,	I_{P}	${\mathbb T}_s$	I 4	T_2	Ip.	Is
10.0	0.61	13.5	0.61	10.0	0.59	13.5	0.59
224.0	1.24	24.5	1.24	22.0	1.23	24.5	1,22
40'.0	2.12	41.0	2.12	40.0	2.10	41.0	2.10
60%0	3,10	61,2	3,13	60.0	3.08	61.2	3.11
80.0	4.16	82.0	4.22	804.0	4.11	82.0	4.16
93.0	4.88	94.2	4.92	92.0	4.74	93.3	4.78
	Circuit	#7		(Circuit	#8	
I'H	VI.	Ip	I,	I,	1.	Ip	\mathcal{I}_s
10.0	0,65	13.5	0.65	10.0	0.60	13.5	0.60
224.0	1.23	24.5	1.23v	22.0	1,25	24.5	1.23
40'.0	2.12	41.0	2.12	40.0	2.09	41.0	2'.10
60',0	3.13	61.2	3.15	60.0	3.09	61.2	3.12
80.0	4.18	82.0	4,25	80.0	4.17	82.0	4.23
95.0	5.0	96.2	5.01	95.0	4.96	96.2	4.98
	Circuit	#10		(Circui #	±11	
I'H	I2	Ip	Is	ΙH	I,	Ιρ	Is.
10.0	0.60	13.5	0.60	20.0	1.08	22.8	1.08
20.0	1.09	22.8	1.09	40.0	2.08	41.0	2.10
40.0	2.08	41.0	2.10	60.0	3.09	61.2	3.13
604.0	3.05	61.2	3.09	80.0	4.14	82.0	4.17
8040	4.05	82.0	4.10	90.0	4.64	91.3	4.69
90.0	4.64 4.95	91'.3 96.2	4.69 4.97	95.0	4.95	96.2	4.97
90.0	4,50	30.6	生•31				

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Ratio Readings.

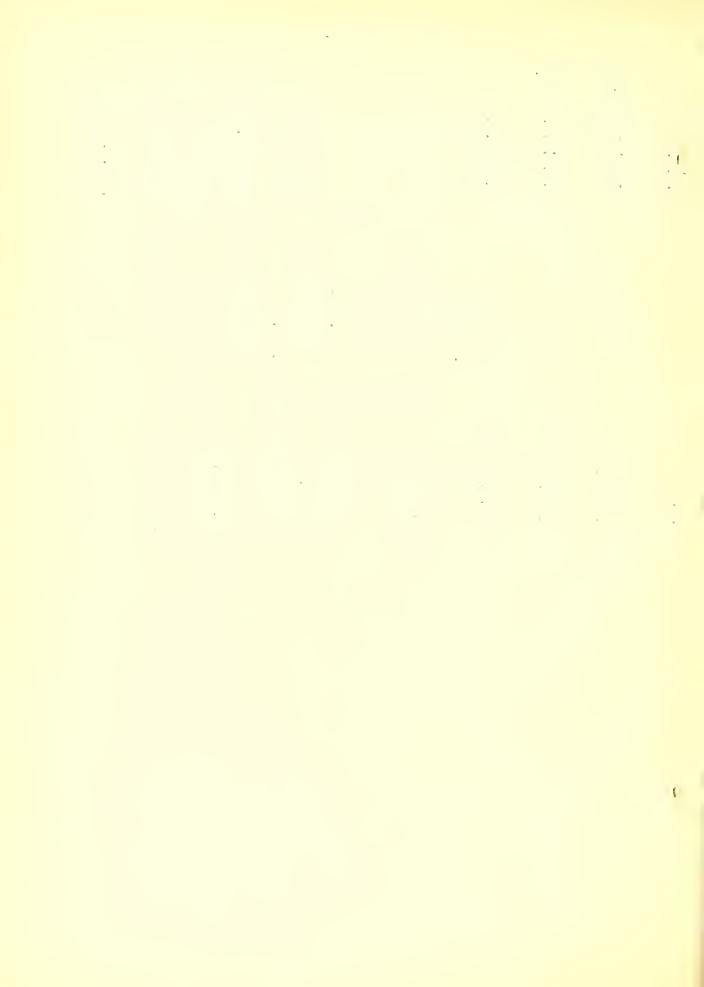
	Circuit	#12.			Circuit	; #13.	
Ιμ	I_{a}	Ip.	I_s	I,	I_2	Ip	\mathcal{I}_{s}
10.0	0.600	13.50	0.600	10.0	0.600	13.50	0.600
20.0	1.146	22.80	1.125	22.0	1.220	24.50	1.210
17.0	2.100	41180	2.100	40.0	≥.050	41.00	2.050
0.0	3.065	61.20	3.095	60.0	F.055	61.20	3.080
80.0	4.070	82.00	4.120	80.0	4.060	82.00	4.110
95.0	4.900	96.20	4.920	93.0	4.810	94.20	4.840

Resistance #1~.

I	臣	#1	#E	R
1	0.222	0.99	0.210	.2125
2	0.430	1.98	0.420	.2120
3	0.635	2.90	0.625	.2110
4	0.847	3.89	0.830	.2130
5	1.055	4.86	1.030	.2120

Impedance #13.

I,	Εμ	Alt.	# I,	I HW.	Ι _ζ	E	Z
1.283 2.500	40.0	50.50 50.50	1.280 2.520	1.240 2.440	.041	0.076 .117 0.229 0.280	2.93 2.88



R.=.0906

L=.000346

T) Iph	I ₂	Defl.	K	I#ph	$\# I_{\mathcal{S}}$	Sin.a	I_p	R	Alpha
4.49 4.54 4.48 4.44 4.47 4.42 4.42 4.43 4.43 4.49	0.20 0.30 0.62 0.85 1.0 1.18 1.33 1.47 1.63 1.72 1.83 1.94	4.0 7.5 12.0 14.0 16.0 18.5 21.0 23.2 25.0 27.5 29.0	76.10 79.00 80.80 81.40 81.80 82.00 82.70 83.00 83.20 83.50 83.65 83.75	4.55 4.60 4.54 4.52 4.50 4.53 4.485 4.48 4.50 4.58 4.49 4.55	0.180 0.288 0.525 0.850 1.000 1.190 1.338 1.476 1.650 1.738 1.850 1.960	.0643 .0717 .0623 .0448 .0435 .0418 .0422 .0422 .0405 .0413	1.8 6.0 11.2 18.0 21.1 25.1 28.2 31.0 34.4 36.0 38.1 40.1	10.00 20.83 21.32 21.18 21.10 21.10 21.08 21.00 20.84 20.70 20.58 20.45	3 41.2 4 06.7 3 34.3 2 29.5 2 23.7 2 25.0 2 25.0 2 23.3 2 23.3 2 25.0
4.48 4.38 4.41 4.45 4.40 4.42 4.42 4.42 4.46	2.05 2.32 2.50 2.73 2.98 3.55 4.23 4.57	33.0 33.5 37.5 39.3 42.0 45.0 49.5 53.5 61.5 65.4	84.00 84.05 84.35 84.45 84.50 84.55 84.35 84.35 84.30	4.54 4.45 4.49 4.46 4.48 4.48 4.52	2.050 2.250 2.350 2.530 2.765 3.015 3.600 2.925 4.285 4.650	.0392 .0378 .0379	42.1 46.0 48.0 51.4 55.6 60.6 65.4 72.0 78.0 91.3	20.50 20.45 20.41 20.30 20.10 20.07 20.04 20.00 19.89 19.81	2 17.2 2 23.3 2 21.6 2 17.5 2 16.2 2 17.5 2 14.8 2 10.0 2 10.3 2 07.2

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Circuit #3

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	R,	206					L =	.00107	2
· Iph	I	Defl	. K	#I _{Ph}	#I.	Sin.a	I_p	R	Alpha
4.45 4.44 4.45 4.46 4.46 4.46 4.47 4.48 4.47 4.48 4.49 4.48 4.31	0.20 0.40 0.63 0.87 1.11 1.28 1.50 1.67 1.98 2.42 2.65 3.03 3.57 3.90	6.0 11.0 14.0 17.0 19.8 21.5 25.0 27.0 30.8 35.5 39.2 42.5 48.0 50.0	78.20 80.40 81.22 81.90 82.40 82.70 83.15 83.40 83.85 34.33 84.40 84.50 84.60 84.58	4.50 4.51 4.51 4.51 4.51 4.52 4.53 4.53 4.53 4.53	0.180 0.390 0.65 0.870 1.112 1.285 1.511 1.690 2.000 2.450 2.675 3.675 3.620 3.960	.0944 .0779 .0612 .0570 .0478 .0450 .0443 .0425 .0406 .0379 .0384 .0360 .0346 .0339	2.25 9.00 13.8 19.0 24.0 27.2 31.2 35.2 40.9 49.5 53.8 61.1 71.3 77.5	12.50 23.10 22.10 21.85 21.85 21.15 20.80 20.82 20.45 20.20 20.10 19.85 19.70	5 25.2 4 28.0 3 30.2 3 02.3 2 14.5 2 33.4 2 26.1 2 19.6 2 10.3 2 12.0 2 03.8 1 59.0
4.37	4.30	55.0 57.0	84.50 84.48	4.43 4.50	4.350	.0337	84.5 90.6	19.40	1 56.0
4.40	5.00	65.3	84.32	4.50	5.000	.0334	96.5	1.9 . 30	1 54.8

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Circuit #4.

7)

R,=.3546 L = .003586 #IPh #I3 Iph IZ Defl. KAlpha Sir.a Ip 4 50.2 4.60 0.30 9.0 79.75 4.63 0.288 6.0 .20.84 .0843 0.75 0.745 4.62 14.8 81.40 4.65 .0525 20.81 3 00.5 15.5 4.68 0.98 81.80 4.70 0.980 20.6 16.5 .0437 21.02 2 30.3 27.2 32.0 82.60 1.285 4.62 1.28 21.0 4.65 26.8 .0427 21.16 2 85.05 2 4.60 1.55 24.0 4.63 1.560 .0400 20.50 17.5 2 10.0 2 05.8 4.60 1.88 27.8 83.50 4.63 1.900 .0378 38.5 20.25 31.5 32.5 4.52 2.17 83.90 2.200 44.3 4.57 .0376 20.18 4.00 2.38 4.63 2.410 1 84.00 .0346 19.98 48.2 59.0 4.70 39.5 4.72 2 01.0 2.825 20.00 2.80 34.40 .0352 56.5 3.305 1 57.6 1 52.8 1 54.2 3.28 4.71 4.73 45.6 84.56 4.0342 65.5 19.71 47.5 3.540 10328 .0332 4.72 3.60 84.58 4.74 71.5 19.64 4.73 3.92 53.0 84.55 4.75 78.0 19.61 4.73 4.42 58.0 84.45 4.75 4.475 .0524 87.0 19.44 1 51.4 4.72 84.35 4.74 4.75 62.5 4.80 .0325 93.0 19.37 1 51.7

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Circuit #5.

R 3	3546	
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L=.0058

Iph	Iz	Defl.	K	#I,ph	#I3	Sin.a	I_p	R	Al ha
4.87 4.91 4.90 4.90 4.90 4.80 4.87 4.83 4.83	0.30 0.85 1.27 1.80 2.35 3.14 3.58 4.12 4.40 4.75	14.5 19.5 25.0 32.2 40.0 49.6 55.5 61.0 65.0 70.8	81.22 82.35 83.18 83.10 84.42 84.60 84.50 84.30 84.20	4.87 4.90 4.90 4.89 4.89 4.89 4.88 4.83 4.83	0.29 0.85 1.27 1.80 2.36 3.16 3.62 4.17 4.45 4.78	.1265 .0570 .0483 .0435 .0412 .0379 .0372 .0357 .0358	35.60 42.20 61.60 70.50 81.00 86.00	20.05 19.78 19.55 19.50	7 16.0 3 16.0 2 46.0 2 29.0 2 22.0 2 10.0 2 08.0 2 02.8 2 03.2 2 06.0

Circuit #6.

				OTTOOT	0 77 0 •					
	R:	.3546				L=.0228				
	1.0	.0010								
Iph 4.90 4.92	0.30 0.78	Defl. 8.2 12.0	K 79.40 80.70	#IPA 4.89 4.91	#Is 0.29 0.77	Sin.a .0729 .0390	I _p 6.5	R 22.40 21.20	Alpha 4 11.0 2 15.0	
4.88 4.88 4.89	1.37 1.82 2.15	15.0 18.8 22.0	81.48 82.25 82.73	4.87 4.87 4.88	1.37 1.82 2.16	.0276 .0258 .0251	36.0 42.2	20.10 19.78 19.53	1 35.0 1 29.0 1 26.8	
4.88	2.64	28.8 3 11 8	83.65 83.95	4.87	65 3.10	.0267	5 .0 61.0	19.60	1 32.0 1 26.0	
4.83 4.83 4.85	3.53 4.00 4.48 4.67	36.0 41.0 47.0 49.0	84.25 84.50 84.58 84.60	4.83 4.83 4.85	3.56 4.05 4.52 4.70	.0248 .0249 .0254 .0255	70.2 79.7 88.5 91.5	19.70 19.65 19.52 19.45	1 25.0 1 26.0 1 27.3 1 27.6	

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4.80

4.78

4.48

4.88

69.5 84.25

84.18

73.5

	R.	.1287				L000346						
I_{Ph}	I ₂	Defl.	K	#Iph	#I _J	Sin.a	Ip	R	Alpha			
4:91	0.35	11.5	80.60	4.900	0.35	.0835	7.3	20.90	4 48.0			
4.90	0.88	21.0	82.62	4.890	1.28	.0497	25.6	20.00	2 51.0			
4.89	1.67	31.0	83.85	4.880	1.68	.0450	33.3	19.80	2 35.0			
4.88	2.00	35.5	84.23	4.875	2:.00	.0432	39.0	19.50	2 29.0			
4.87	2,38	41.5	84.50	4.865	2.40	.0421	46.5	19.35	2 25.0			
4.88	2.90	49.0	84.60	4.875	2.93	.0406	57.0	19.45	2 19.5			
4.82	3.32	54.0	84.55	4.820	3.37	.0395	65.5	19.40	2 15.1			
4.80	3.70	59.0	84.45	4.805	3.75	.0383	72.5	19.32	2 13.0			
4.80	4'.00	62.5	84.35	4.805	4.05	.0380	78.2	19.30	2 10.6			

4.805 4.52

4.850 4.92

.0379 87.2

94.5

.0366

19.28

19.20

2 10.31

2 05.9

Circuit #8 R .. 2292 L=.000346 IPh I, #IPS $\#I_s$ Defl. K Sin.a R Alpha I_p 4.93 0.35 13.0 4.915 0.35 7.8 5 21.0 81.00 .0931 22.30 4.875 4.88 0.88 82,28 3 05.0 19.0 0.88 .0538 20.70 18.2 1.33 4.91 25.0 .83.15 4.900 1.33 .0461 27.0 20.30 2 38.0 2 33.0 4'.91 1.70 31.0 83.85 4.900 1.70 34.0 20,00 .0444 4.91 2.13 37.5 84.33 4.900 2.14 19.60 2 26.0 .0424 42.0 2 13'.0 2 09,0 4.91 2,55 41.0 84.48 4.900 2.56 .0387 50.2 19.60 4.90 84.58 3.02 3.00 46.8 4.890 .0374 59.0 19.54 84,53 84,37 19.55 4.89 3.50 54.5 4.880 3.54 .0373 69.3 2 02.0 4.90 4.00 62.0 4.890 4.05 78.8 19.45 2 07.0 .0371 4.39 84,25 4.93 1 .35 4,52 68.0 4.880 .0335 95.5 1 55.0 4.90 4.925 73.5 84.18 4.890 4.94 19.35 2 04.0 .0361 95.6

C	i	r	C	u	i	t	#10
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	$R_{\mathfrak{g}}$:	.259					Ji ± .	000346	
I _{Ph}	I_2	Dekl.	K	#Ip4	#I3	Sin.a	IP	R	Alpha,
5.00 4.95 4.94 4.91 4.92 4.92 4.93 4.93 4.93 4.93 3.93 3.93 3.93 3.93	0.35 0.62 1.04 1.22 1.52 1.82 2.035 2.75 2.98 3.50 3.50 4.01 4.20 4.67 4.95	16.0 21.0 22.0 23.5 35.5 40.5 46.5 54.6 55.6 48.0 52.0 57.0 59.5 59.5 59.5 59.5 59.5 59.5 59.5 59	81.70 82.65 83.40 83.55 84.05 84.33 84.40 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.55 84.60	4.98 4.91 4.93 4.90 4.90 4.91 4.91 4.91 4.91 4.91 4.91 4.91 4.91	0.61 1.04 1.23 1.53 1.80 2.04 2.29 2.54 2.79 3.28 3.57 3.55 3.55 4.225 4.55 4.725	.1121 .0847 .0635 .0554 .0525 .0482 .0457 .0423 .0413 .0398 .0369 .0369 .0366 .0366 .0366 .0350 .0350 .0352 .0346	7.5 13.2 22.0 26.0 31.5 37.0 42.0 51.2 56.0 65.2 70.8 70.5 79.6 89.0 99.0	21.40 21.20 21.20 20.60 20.55 20.30 20.15 20.65 19.90 19.85 19.65 19.65 19.65 19.45	6 26.2 4 59.5 3 38.5 3 10.6 3 00.5 2 46.0 2 25.6 2 22.0 2 17.0 2 13.7 2 07.0 2 06.0 2 03.3 2 00.0 2 01.0 1 59.0

(li	r	C.	U	i	10	#11
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R. 3546

I _{Ph}	Iz	Defl.	K	$\# \mathbf{I}_{PA}$	$\#I_s$	Sin.a	Ip	R	Alpha
4.91	0.58	13.5	81.10	4.90	0.575	.0592	13.0	22.60	3 23.6
4.92	1.00	19.2	82.30	4.91	1.000	.0475	21.5	21.50	2 43.3
4.87	1.52	23.5	82.98	4.87	1.463	.0398	30.8	21.05	2 16.9
4.94	2.03	29.5	83.70	4.93	2.040	.0350	41.8	20,50	202.0
4.96	2.55	37.0	84.30	4.95	2.550	.0338	51.5	20.20	1 59.6
4.90	2.95	41.5	84.50	4.95	2.988	.0332	59.8	26.00	1 54.3
4.86	3.54	48.0	84.60	4.86	3.585	.0326	71.0	19.80	1 52.0
4.90	4.00	52.0	84.57	4.89	4.060	.0309	79.8	19.65	1 46.2
4.88	4.50	59.5	84.40	4.88	4.525	.0319	88.5	19.55	1 49.7

L=.009626

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Circuit #12.

R.:.212

L = .000346

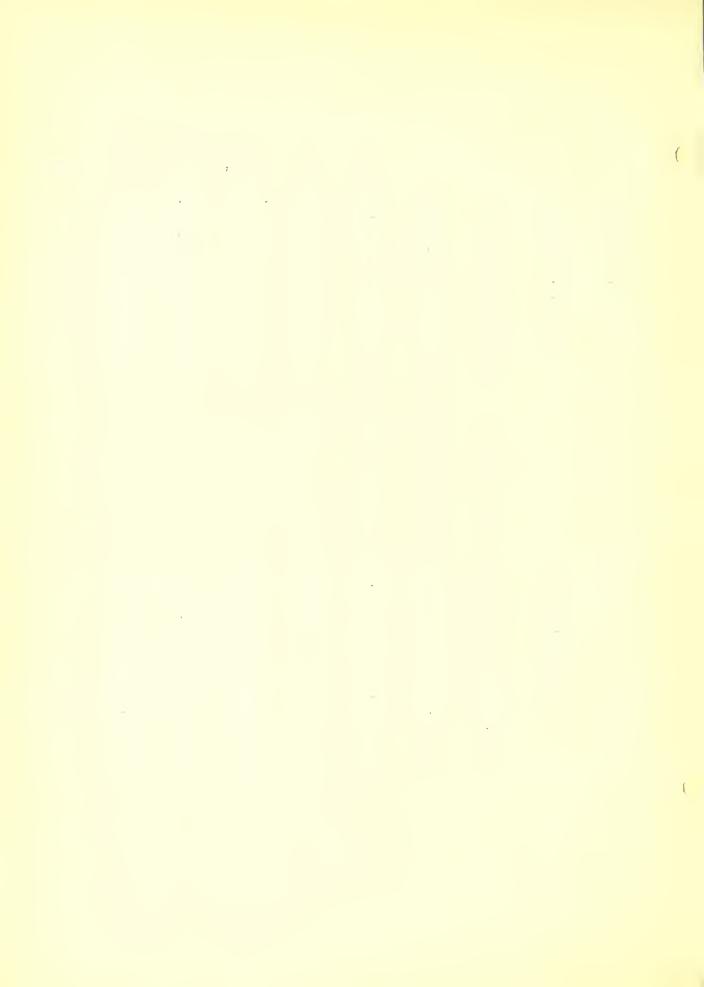
I_{Ph}	I_{σ}	Defl.	K	$\#I_{ph}$	#1,	Sin.a	I_{ρ}	R	Theta
4.92 4.90 4.89 4.92 4.90 4.91 4.80 4.90 4.88	0.35 0.80 1.32 1.67 2.00 2.57 3.00 3.51 4.02 4.50 4.97	10.0 16.5 23.5 28.5 33.0 40.0 46.0 51.5 57.0 65.0 70.0	80.13 81.80 82.98 83.60 84.03 84.44 84.58 84.49 84.30 84.22	4.90 4.89 4.88 4.90 4.89 4.90 4.89 4.80 4.89 4.87	0.35 0.80 1.32 1.69 2.00 2.58 3.02 3.55 4.07 4.55 4.99	.0728 .0518 .0440 .0411 .0401 .0375 .0368 .0350 .0345 .0346	7.5 16.7 17.2 34.5 40.5 51.8 60.2 70.5 80.8 89.6 97.8	21.40 21.00 20.62 20.40 20.25 20.08 19.93 19.85 19.68 19.60	4 10.0 2 58.0 2 31.0 2 21.0 2 18.0 2 09.0 2 06.5 2 01.0 1 58.5 1 59.0 1 57.5

Circuit#13.

R_j=.3546

L=.0166

I _F	$\mathbf{I}_{\mathcal{S}}$	Defl.	K	#Iph	$\#I_s$	Sin.a	I_{ρ}	R	Theta
4.91 4.86 4.88 4.88 4.87 4.88 4.87 4.85 4.81	0.35 0.85 1.28 1.28 1.98 2.41 3.03 3.55 3.98 4.50 4.80	7.3 13.8 19.5 22.5 26.0 30.5 38.6 43.5 50.8 54.5 57.5	79.00 81.20 82.37 82.32 83.30 83.81 84.40 84.52 84.58 84.58	4.90 4.86 4.87 4.87 4.86 4.87 4.86 4.81	0.35 0.85 1.29 1.65 2.00 2.42 3.05 2.58 4.55 4.88	.0538 .0412 .0378 .0338 .0321 .0310 .0308 .0295 .0307 .0291	7.5 18.0 26.8 34.0 40.8 48.8 61.0 70.0 79.5 89.0 94.0	21.40 21.18 20.85 20.62 20.42 20.22 20.00 19.55 19.70 19.56 19.50	3 03.0 2 22.0 2 10.0 1 56.0 1 50.0 1 47.0 1 46.0 1 41.0 1 45.0 1 40.0



Circuit #1.

					igle Er		Tota	al Error	r.
I_{ρ}	Ratio	Alph:	Ratio	100/3	86.7	64?3,		86.7	54.3,6
10 20 30 40 50 60 70 80 90	21.30 21.15 20.95 20.30 20,35 20.15 20.00 19.90 19.72 19.50	3 27.0 2 54.0 2 23.0 2 20.0 2 18.0 2 15.5 2 13.0 2 11.3 2 09.0 2 07.0	6.50 5.75 4.75 3.00 1.75 0.75 0.00 -0.50 -1.40	PF. .181 .100 .087 .083 .081 .075 .075 .069	2.75 2.75 2.50 2.40 2.30 2.30 2.25 2.20	7.45 5.55 5.20 5.20 5.00 4.90 4.75 4.10 4.60 4.50	6.681 5.850 4.837 3.083 1.831 0.888 0.075 -0/427 -1.331 -2.432	10.2	P
			(Circui	t #3.				
10 20 30 40 50 60 70 80 90	22.85 21.60 20.92 20.50 20.20 19.92 19.70 19.36 19.36	3 54.0 2 58.0 2 32.0 2 19.0 2 10.0 2 03.5 1 59.0 1 55.5 1 53.0 1 51.0	14.25 8.0 4.60 2.50 1.00 -0.40 -1.50 -2.50 -3.20 -3.60	.232 .134 .098 .082 .071 .063 .060 .056	4.30 3.10 2.70 2.50 2.40 2.25 2.20 2.15 2.05 2.00	8.30 3.55 5.35 4.90 4.50 4.20 4.10 3.90 3.80	14.485 8.134 4.698 2.582 1.071 337 -1.440 -2.444 -3.146 -3.548	16.55 11.10 7.30 5.00 3.40 1.85 0.70 -0.35 -1.15 -1.60	22.55 14.55 9.95 7.40 5.50 3.90 2.70 1.60 0.70 0.20
			(Circui	t #4.				
16 20 30 40 50 60 70 80 90	23.02 20.70 20.41 20.16 19.95 19.79 19.68 19.63 19.62	3 36.5 2 44.0 2 20.5 2 08.5 2 01.0 1 56.0 1 54.0 1 52.0 1 52.0	15.00 3.50 2.05 0.80 -0.25 -1.07 -1.60 -1.85 -1.90 -1.90	.198 .114 .083 .069 .062 .057 .055 .053	4.00 3.90 3.50 3.130 3.20 3.15 3.10 3.05 3.05	7.65 6.50 5.00 4.50 4.30 4.20 4.10 3.90 3.90 3.90	5.29° 3.614 2.133 0.869 -0.188 -1.013 -1.545 -1.797 -1.847	9.10 7.40 5.55 4.10 2.95 2.08 1.50 1.20 1.15	12.75 10.00 7.05 5.30 4.05 3.13 2.50 2.05 2.00

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Circuit #5.

					igle Er	ror		otal Er	ror .
I	Ratio	Alpha . /	Ratio Error	100°s	26Q7 P.F.	64.3% P.F.	100; P.F.	86.7,0 P.F.	64.3% P.F.
10	50.58	51	2.60	0.52	6.50	12.8	5.12	9.10	15.40
20 3 0	20.15	3 05 2 38	0.75 -0.50	0.15	3.40 2.80	6.9 5.7	0.90	4.15 2.30	7.55 5.20
40 50	19.70	2 25 2 18	-1.50 -2.15	90.0	2.70	5.3 5.2	-1.41 -2.07	1.20	3.80 3.05
60	19.50	2 12	-2.50	0.08	2.40	5.0	-2.42	-0.10	2.50
70 80	19.46	2 08 2 02	-2.70 -3.00	0.07	2.30	4.7	-2.94	-0.40 -0.80	2.00
90	19.25	1 56	-3.75	0.06	2.10	4.3	-3.39	-1.65	0.55
100	19.00	1 52	-5.00	0.05	2.00	4.0	-4. 95	-3.00	-1.00
		ر د		Circui	t #6				
10	21.95	3 20	9.1,8	0.17	5.70	7.2	10.05	17.58	17.08
20 30	20.75	1 54 1 33	5.75 -Q.50	0.06	2.00	4.3	3.81 -0.45	5.75 1.30	8.05
40	19.70	1 27	1.50	0.03	1.70	3.2	-1.47	0.20	1.70
50 60	19.63 19.65	1 26 1 26	-1.85 -1.75	0.03	1.60	3.00	-1.82 -1.72	-0.25 -0.15	1.15 1.25
70 80	19.70 19.65	1 26 1 26	-1.50 -1.75	0.03	1.60	3.0	-1.47 -1.72	0.10 -0.15	1.50 1.25
90	19.50	1 27	-2.50	0.03	1.70	3.2	-2.47	-0.80	0.07
100	19.30	1 28	-3.50	0.03	1.80	3.3	-3.47	- , ^r /0	-0.20
		0 /		Circui	#7.				
10	20.70	4 24	3.50	0.19	4.80	9.5	3.79	8.30	13.00
20 30	20.15	3 12 2 41	0.75 -0735	0.16	3.50 3.00	5.7	0.91	4.25 2.25	7.45 5.05
40	19.65	2 28	-1.75	0.09	2.70	5.3	-1.66	0.95	3.55
50 60	19.52	2 22 2 18	-2.40 -2.95	0.09	2.50	5.2 5.1	-2.51 -2.87	0.10	2.80 +2.05
70	19.35	2 14	-3.25	0.08	2.30	4.9	-3.13	-0.95 -1.30	+1.65 1.20
80 90	19.28 19.22	2 11 2 08	-3.60 -3.90	0.07	2.30	4.8	-3.53 -3.83	-1.60	0.80
100	19.18	2 06	-4.60	0.07	2.20	4.5	-4.53	-2.40	-0.10
				Circui	it #8.				
10	21.71	4 27	8.75	0.30	4.30		9.05	13.55	18.25
20 30	20.62	3 OL 2 37	3.10 0.40	0.13	3.20 2.80	6.5 5.7	3.23 0.50	3.20 3.20	9.60 6.10
40	19.95	2 24	-0/25	0.09	2.40	5.3	-0.13	2.15	5.00
50 60	19.56	2 15 2 11	-2.20 -2.50	0.08	2.30	4.9	-2.12 -2.43	0.10	2.70
70	19.48	2 08	-2.60	0.07	2.30	4.7	-2.53 -2.68	-0,30 -0.55	2.10 1.85
80 90	19.45	2 07 2 06	-2.75 -3.00	0.07	2.20	4.5	-2.93	08.04	1.50
100	19.30	2 04	-3.50	0.07	2.15	4.4	-3.43	-1.35	0.90

Circuit #10.

				А	ngle E	rror	7ºot	al drro	r .
I	Ratio	_	Ratio Error	100	86.7	64.3%	100	85.75	34.35
10	21.50	5 44	7.50	P.F. .500	P.F. 6.25	P.F. 12.3	P.F. 8.000	P.F. 13.75	P.F. 19.30
20 30	20.98	3 57 3 0 7	4.90	.232 .148	4.20	8.6 6.7	5.138 3.898	9.10 7.00	13.50 10.45
40	20.37	2 39	1.85	.107	2.75	5.7	1.957	4.60	7.55
50 60	20.16	2 23 2 14	0.80	.087 .075	2.40	5.0 4.8	0.887	3.20 2.10	5.50 4.60
70	19.80	2 09	-1.00	.069	2.23	4.5	-0.931	1.23	3.50
80 9 0	19.65 19.50	2 04 2 01	-1.75 -2.50	.063 .062	2.22	4.4	-1.687 -2.438	0.47	2.65 1.90
100	19.35	1 59	-3. 25	.060	2.20	4.3.	-3.190	-1.05	1.05
		•		Circui	t #11.				
10	23.00	3 48	15.00	.210	4.05	8.10	15.210	19.05	23.10
20 30	21.84	2 49 2 19	9.20 5.30	.121	2.95 2.45	6.6 5.0	9.321 5.082	12.15	15.80
40 50	20.57	2 04	2.85 1.15	.063	2.20	4.5	2.913	5.05	7.30
60	19.99	1 54	-0.05	.057 .055	2.15	4.2	0.005	2.07	5.45 4.15
70 80	19.81	1 50 1 49	-0.95 -1.75	.051 .050	2.10	4.0	-0.899 -1.700	1.15 0.25	3.05 2.15
90	19.55	1 49	-2.25	.050	2.00	3.9	-2.200	-0.25	1.65
100	19.44	1 49	-2.80	.050	2.00	3.9	-2.750	-0.80	1.10
				Circui	t #12.				
10	21.29 20.85	3 39 2 47	6.45	.203	4.00	7.7	6.653	10.45	14.15
20 30	20.52	2 26	4.25	.118	2.95 2.55	5.9 5.2	4.368 2.690	7.20 5.15	10.15
40 50	20.25	2 15 2 08	1.25	.077	2.45	4.8	1.327	3.70 2.75	6.00 4.90
60	19.97	2 03	-0.15	.065	2.20	4.3	-0.086	2.05	4.15
70 90	19.86	2 00	-0.70 -1.00	.061	2.15	4.3	-0.539 -0.940	1.45	3.55 3.20
90	19.70	1 58 1 57	-1.50 -2.15	.059	2.05	4.2	-1.441	0.55 -0.15	2.65
100	75.01	T 97	=	.058	2.00	4.1	-2.092	-U .IJ	1.95
				Circui	t #13.				
10	21.37	2 5	6.85	.125	3.00	6.0	6.975	9.85	12.85
20 30	21.09	2 20 2 00	5.45	.038	2.50	4.9	5.533	7.95	10.40
40				.061 .051	2.15	4.3 3.6	3.611	5.70 3.90	7.80 5.60
	20.40	1 50	2.00						
50	20.15	1 47	0.30	.048	1.80	3.6	0.848	2.60	4.40
50 6 0 70	20.15 19.96 19.80	1 47 1 45 1 44	0.80 -0.20 -1.00	.048 .047 .046	1.80 1.75 1.74	3.6 3.6 3.5	0.848 -0.154 -0.954	2.60 1.55 0.74	4.40 3.25 2.54
50 60	20.15 19.96	1 47 1 45	0.80 -0.20	.048	1.80	3.6 3.6	0.848	2.60	4.40 3.25

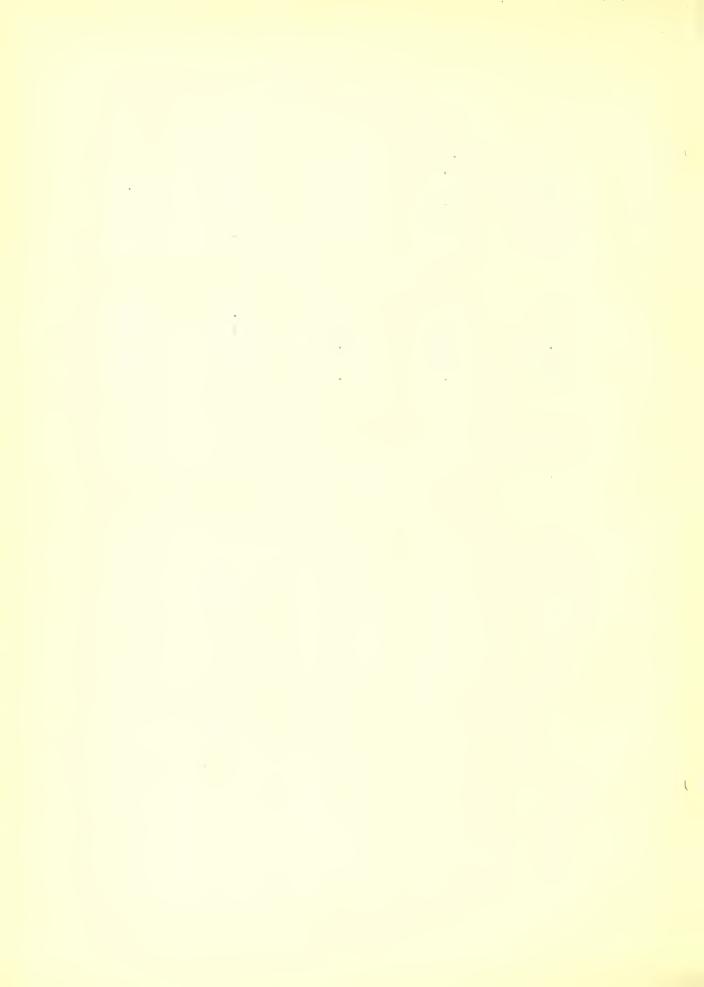
Ratio Readings.
Constant Res**is**tance.

Circuit	4	<u>5</u>	11	13	<u>6</u>
I r 20 40 60 80 100	20/70 20.16 19.79 19.63 19.62	20.15 19.70 19.50 19.40 19.00	RATIO 21.84 20.57 19.99 19.65 19.44	21.10 20.40 19.96 19.65	20.75 19.70 19.65 19.65
		Constant	Rea	actance.	
Circuit 20 40 60 80	1 21.15 20.60 20.15 19.90 19.50	7 20.15 19.65 19.41 19.28 19.18	12 20.88 20.25 19.85 19.80 19.55	8 20.62 19.95 19.50 19.45 19.30	10 20.98 20.37 19.97 19.65 19.35

Angle Readings.

Constant Resistance.

Circuit 20 40 60 80 100	2 44 2 09 1 56 1 52 1 52	5 05 2 2 2 1 52 12 2 152	2 20 2 04 1 54 1 49 1 49	13 2 49 1 50 1 45 1 43 1 42	6 1 54 1 27 1 26 1 27 1 28
20 40 60 80 100	2 34 2 20 2 16 2 11 2 07	Constant 7, 3 12 2 28 2 18 2 11 2 06	Re ,/2, 2 47 2 15 2 04 1 59 1 58	3 01 2 24 2 11 2 07 2 04	3 57 2 39 2 14 2 04 1 59



Errors for 80, Power Factor.

	Const	ant R.	Va	riable L.		
<u>L</u>	.0050	.0075	.0100	.0150	.0175	.0200
		20		Was Provident days of the co.		
Ratio Alpha Total	1.25 4.20 5.45	4.80 4.20 9.00	Amper: 8.15 3.70 11.65	6.60 3.20 9.80	5.40 3.00 8.40	4.50 2.80 7.30
Ratio Alpha Total	-0.90 3.10 2.10	-0.50 3.00 2.50	Ampere 2.60 2.70 5.30	2.65 2.50 5.15	1.60 2.40 4.00	-1.50 2.00 0.50
Ratio Alpha Total	-1.40 2.80 1.40	-0.85 2.70 1.85	Ampere: 0.00 2.50 21,50	0.25 2.40 2.65	-0.25 2.30 2.05	-1.75 2.00 0.25
Ratio Alpha Total	-2.90 2.60 -0.30	-2.65 2.50 -0.15	Ampere -1.90 2.40 0.50		-1.60 2.30 0.70	-1.75 2.00 0.25
Ratio Alpha Total	-3.40 +0.90 -0.90	-3.60 2.50 -1.10	Ampere -2.95 2.40 -0.55	-2.85 2.30	-2.95 2.30 -0.65	-3.45 2.00 -1.45
	Cons	tant L.	Va	ariable R.		
R	0.09	0.12	0.18	0.2	20	.024
Patio Alpha Total	5.65 3.50 9.16	1.50 4.30 5.80	-0.50 4.20 3.70	4.8	30	3L15 4.50 7.70
Ratio Alpha Total	4.00 3.20 7.20	40 -1.25 3.30 2.05	Ampere -2.38 3.20 0.88	5 -1.7 3.0	0	0.50 3.30 2.80
Ratio Alpha Total	0.75 3.00 3.75	60 -2.25 3.20 0.95	Ampera -3.50 2.80 0.70) -3.3) 2.7	0	1.75 2.90 1.25
Ratio Alpha Total	-0.50 +2.90 2.40	-3.10 3.00 -0.10	Amper -4.28 2.70 -1.58	5 -z.9 2.6	60	2.50 2.80 0.30



Data for Calibration Curves.

Hot Wire with Shunt.			ot Wire :	no unt.		Hot Wire Against I ₂		
13.2 23.0 31.0 41.5 51.0 631255 71.5 81.75 92.0	10.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0	0. 0. 1. 1. 2. 2.	92 25 54 85 15 43 71	10.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0	I ₂ 0.75 1.25 1.655 2.00 2.415 2.97	I, 0.70 1.25 1.705 2.005 2.43 2.98		
Hot Wir			alibration of E	on		meter 03.		
14.3 23.2 35.0 41.6 56.8 69.5 78.2 93.0 101.0	E.7037 .061 .093 .111 .150 .184 .215 2255 .280	.0 .0 .1 .1	E _y , 30 60 00 30 60 00 30	EM. .032 .063 .105 .132 .165 .208 .235 .267 .308	E. C. 30 0.40 0.60 0.80 1.00 1.50 2.00	0.31 0.41 0.61 0.82 1.015 1.515 2.065		
	eter agains and I _{ph}	t		n. as eter.	Amae 10			
D. 13.5 15.0 17.0 20.0 21.8 24.0 27.0 29.0 31.30 33.5	2.915 3.150 3.340 3.630 3.860 4.050 4.230 4.490 4.700 4.850	2.90 3.15 3.34 3.62 3.84 4.05 4.28 4.49 4.69 4.84	5.50 7.00 10.20 12.35 14.50 16.85 19.70 22.20 25.60 28.50 32.00 55.25	2.00 2.25 2.75 3.00 3.26 3.50 3.75 4.00 4.25 4.50 4.75 5.00	1.00 2.00 3.00 4.00 4.86	I 1.00 2.03 3.06 4.10 5.00		

• . • . .

Ratio Readings for Transformer #2.

25 Ampare Chunt used.									
#	1.	#3		-				#1	1.
IH	I_2	IH	I,	I H	I>	IH	I	Ι _Η	IL
3.0	0.70	2. 5	0.65	2 2.5	0.56	3.0	0.74	2.5	61
5.0	1.17	6.5	1.44	5.0	1.13	5.0	1.16	5.0	1.12
10.0	2.13	10.0	2.12	10.0	2.09	10.0	2.13	10.0	2.09
12.5	2.62	12.5	2.59	12.5	2.58	12.5	2.62	12.5	2.59
15.0	3.15	15.0	3.13	15.0	3.12	15.0	3.17	15.0	3.11
16.0	3.35	17.5	3.72	17.4	3.65	17.5	3.70	16.9	3.52
	3.73	18.25				19.0	3.98		
	4.20								



Data	on	Transformer	#2.	Phase	Angla.
------	----	-------------	-----	-------	--------

Circuit #1.			Circuit #3.			Ci	Circuit #4.		
Iph	<u>T</u> 2	Defl.	Iph	I	Defl.	Iph		Defl.	
4.90 4.92 4.92 4.90 4.91 4.92 4.89 4.88 3.88 3.88 3.88	0.25 0.82 1.27 1.63 1.92 2.17 2.38 2.72 3.07 3.36 3.60 3.87 4.13 4.32	3.0 13.8 18.2 26L8 30.5 32.0 38.4 42.3 45.5 40.0 43.8 47.8 50.0	5.02 4.90 5.00 4.90 5.02 4.95 4.96 4.95 5.95 5.95 3.95	0.20 0.72 1.14 1.43 1.71 2.05 2.30 2.60 2.95 3.20 3.48 3.75 4.00 4.13	5.2 15.5 21.8 24.5 24.5 30.2 34.2 30.2 46.0 47.5 48.4	5.00 4.96 4.92 4.93 4.93 4.95 4.85 4.86 3.86 3.86 3.80 4.75	0.20 0.55 1.10 1.40 1.70 2.05 2.354 2.75 3.00 3.25 3.52 3.80 3.90 4.00	3.0 11.8 19.8 25.0 32.8 35.5 47.0 49.8 47.0 47.7 48.5	

Circuit #11.

Circuit #10.

Iph	I,	Defl.	Iph	I	Defl.
4.81	0.20	6.0	4.90	0.20	7.0
4.85	0.62	14.5	4.89	0.75	15.0
4.85	1.02	18.5	4.90	1.20	22.5
4.86	1.30	21.5	5.00	1.55	26.5
4.82	1.54	23.0	4.90	1.78	27.5
4.85	1.90	30.8	4.92	2.22	34.8
4.91	2.25	32.5	5.00	2.48	40.0
4.95	2.50	35.8	4.98	2.80	43.2
4.95	2.75	39.5	4.98	3.22	46.5
4.90	3.00	42.0	4.98	3.51	50.5
4.81	7.30	45.5	5.00	3.87	56.0
	3.52	38.5	5.00	4.00	59.4
3.94	0.00	00.0	0.00	-X • O O	000

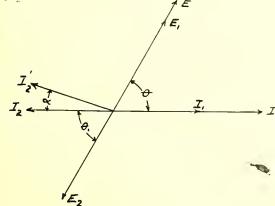




By means of the calibration curves of the various instruments used in the test, the data was corrected, the corrected values being used as the basis of all the curves. The preliminary curves were then drawn for each circuit with the primary current as abscissas and the ratio and the angle alpha as ordinates. From these curves values were picked for additional curves, and for convenience these values were taken for every ten amperes as shown ordata sheets pp.22-25.

From these values the ratio error, angle error, and total error were determined. Evidently the ratio error in percent is equal to 100(apparent ratio- true ratio)/(true ratio), and since the true ratio is 20, the formula resolves itself into ratio error 100(apparent ratio-20)/20. A study of the ratio relations between the primary and the secondary of the series transformer, and the above equation shows that necessarily positive values of error are in favor of the consumer, since more current is favoring than is measured, and hence negative values are in favor of the station.

The percentage angle error may be determined from the formula percent error $100(1-\cos(a\frac{10}{2})/\cos\frac{10}{2})$, where alpha is the error angle as determined in preceding data, and theta is the angle of phase difference between the primary e.m.f. and current. The above equation was determined in the following manner:



Let E=E. N. F. on mains, and I= current in mains, and $\cos\theta=$ power factor. Then the power supplied = $EI\cos\theta$. In the series transformer E, of the primary = KE, and I, of the primary = KI, and $\cos\theta$ is common,



thus E.I. $\cos \theta$ = K.E.I. $\cos \theta$, that is, the power in the primary of the transformer is proportional to the power in the mains. Assuming ideal transformer relations and a ratio of 1 to 1, the platter merely for convenience as any ratio will lead to the same result, the I. I. and is 180 degrees out of phase with it, also E.E. and is 180 degrees out of phase with it, hence, E.I. $\cos \theta$ = E.I. $\cos \theta$ = K.E.I. $\cos \theta$, which states that E.I. $\cos \theta$ is measure of the true power supplied, based on ideal conditions. Due to the resistance and the reactance of the transformer the phase angle difference in the primary and the secondary may differ by some small angle alpha, and hence the power registered on the secondary side would be E.I. $\cos(\theta + a)$, and since E.E. and I.E., the power registered would be E.I. $\cos(\theta + a)$. The error would then be $100(E.I.\cos\theta - E.I.\cos(\theta + a))/E.I.\cos\theta = 100(1 - \cos(\theta + a))/\cos\theta$.

As the angle is a lag angle, the error caused therety is always in favor of the censumer, and is therefore considered a positive error. The alrebraic sum of the ratio error and the angle error gives the total error. It is this tetal error which, is used as ordinates in curves 13-24. A study of the data for these error curves shows that the total error for 100% power factor and the ratio error differ only slightly, so that only the ratio error curve for 100% power factor was plotted.

A series of angle and ratio values were taken from the circuit curve, for 25%, 50%, 75%, 100%, and 125% of full load, grouping those results with the same resistance and variable reactance, and also those with the same reactance and variable resistance. In the first case the angle alpha and the ratio were plotted against the reactance, while in the latter case they were plotted against the resistance.



For points on these curves, the error was calculated and political against resistance and inductance. Circuit #10, the nearest approach to practical conditions, with a resistance equal to that of 100 feet of #14 B.b.S. wire and a low inductance, was then selected, and the total error for different power factors plotted against power factor, for different loads. A sample calculation of the above is shown in the following:

Sircuit #10 on page 20 is taken as the standard because it is the nearest to actual conditions.

I=5.00 #I=4.98 I=0.35 #I=0.35 Defl=16.0 K=81.70 16.0 Sina=----= .1121 a=6° 26.2'

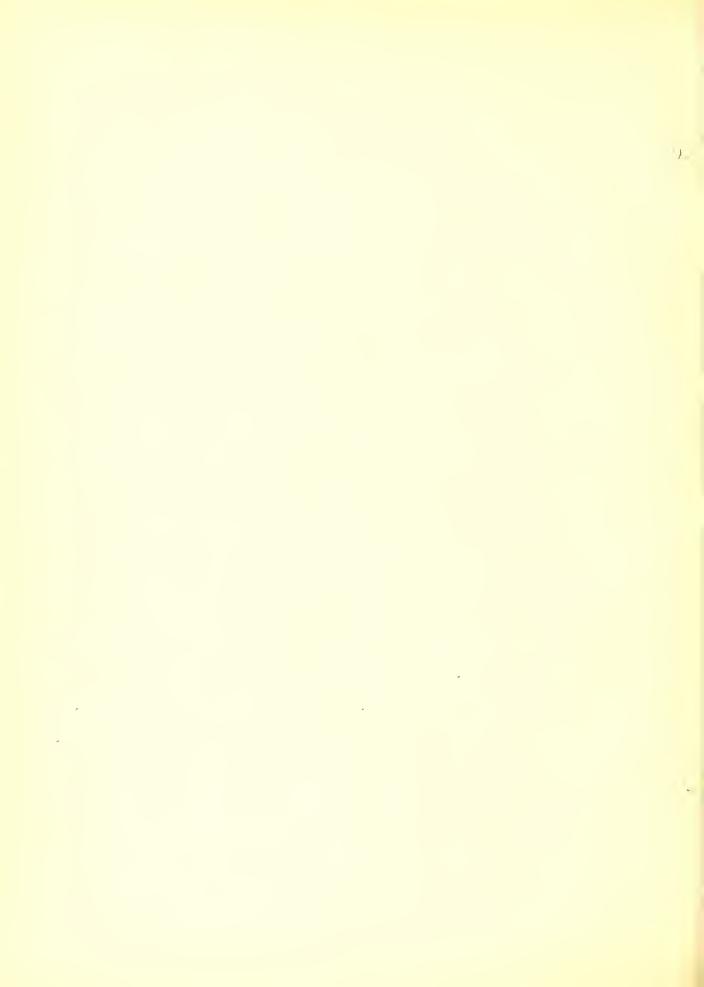
From ratio readings on page 13 a curve was plotted between the primary and secondary currents. Then by taking I_p corresponding to secondary current $I_{\frac{1}{2}}0.35$, a value of $I_{\frac{1}{2}}7.5$ was obtained. This gives a ratio of 7.5/3.5=21.40. These values of ratio and alpha are plotted against I_p on curve sheet $\frac{1}{2}9$. Points picked off of these curves for every ten amperes are tabulated on page 24.

From this data take I_s :20. Then ratio is 20.98 and Serror is 100(20.98 - 20.00)/20 or 4.90%. Alpha for same I_s is 3.57.0.

%Error=100 - 100cos($\frac{\theta}{4}$ + a)/cos $\frac{\theta}{4}$. For an 86.7% power-factor $\frac{\theta}{4}$ =30° and ($\frac{\theta}{4}$ + a)=33°57.0°. Cos $\frac{30^2}{4}$.8295.

This gives an error of 4.2%. Total error is 4.9 + 4.2=9.1% Values obtained as above are plotted against I, on curve sheet 20.

Page 25 gives the values of ratio and alpha for the different circuits where R is constant and L is variable and also where L is constant and R is variable. These plotted against R and L give curve sheets 24 and 25. The errors for the same for 80% power-factor are tabulated on page 25 and the curves plotted from this data are on curve sheets 26 and 27.



A general consideration of the curve sheets show the ollowing conclusions;

Ratio, Angle, - I, Curves.

The ratio and the angle decrease with increased load as does also the error due to these.

Angle - Resistance Jurves.

The angle approaches zero for zero resistance. A maximum angle occurs at .13 ohms. A minium at .20. An increase of load straightens out the curves and tends to make the angle error constant for all resistancees. It also decreases the angle.

Ratio - Resistance Curves.

Transformer circuit has a critical resistance which gives a minimum value to the ratio either a decrease or increase in the resistance raising the ratio. For any resistance an increase in load decreases the value of the ratio. Curves show that there are two resistances that will give the true value to the ratio for any load.

Angle - Inductance Curves.

The abgle decreases with load. The critical value of inductance at which alpha is a maximum is .006 henrys. Any increase or decreasing the inductance decreases this angle.

Ratio - Inductance.

An increase in the inductance lowers the ratio and makes it more constant. For high loads the ratio is nearly constant for all values of L. The curves indicate a critical maximum and a minimum.

Power factor - Error.

The error decreases with an increased power factor.



Resistance - Error Curves.

The total error varies disactly inversely as the load and may be negative. There is a critical value of R which gives a minimum verror.

Inductance - Error Curves.

The total error varies inversely as the load and may be negative.

A critical value of R gives a maximum error.

A consideration of the above shows that the inductance and resistance in the secondary play an important part in the correct operation of the series transformer for switch-board use. Where the instrument leads and transformer are calibrated together and used together the errors shown in the curves are eliminated. But this is not the practice as the position of the instruments may be changed or the resistance of the leads cannot be determined at the time of calibration.

That this is an important consideration is shown by the fact that the errors in some of the circuits approach very large values on light loads and values that cannot be neglected even on the usual operating loads. The average error will introduce a loss to any station sufficiently large to make it worth while for them to investigate this error.

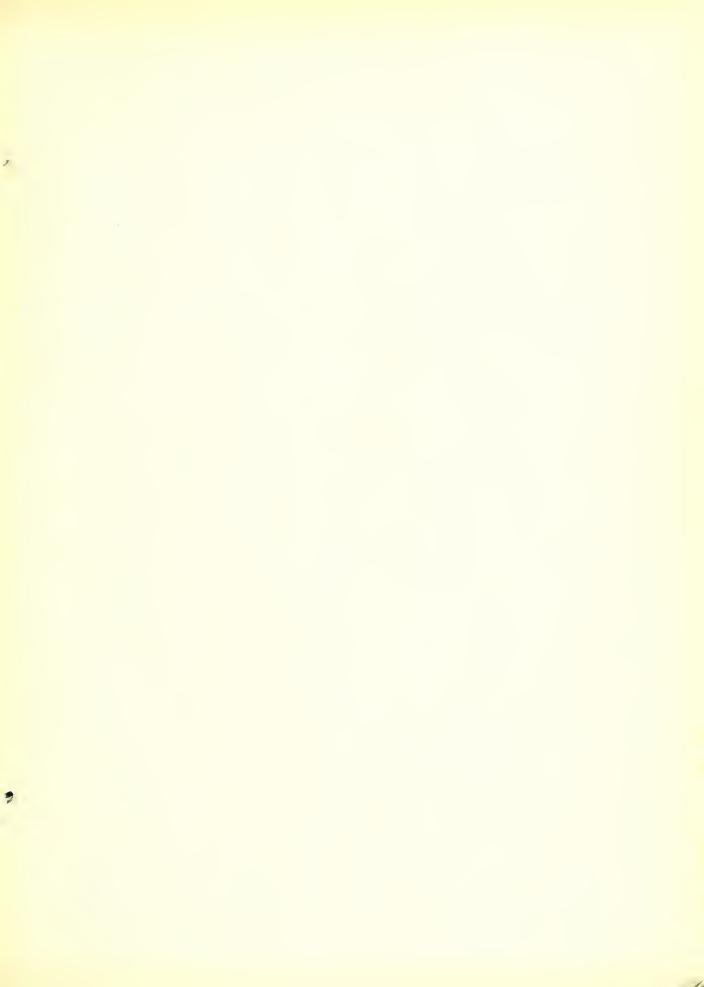
It is customary in making a series transformer test to merely test the ratio of transformation. This of course is made on the aassumption that the current and e.m.f. in the secondary of the transformer bear the same relation to each other that the current and e.m.f. in the primary do, or of not, that the error introduced thereby is negligible. That this is a serious mistake will be noted



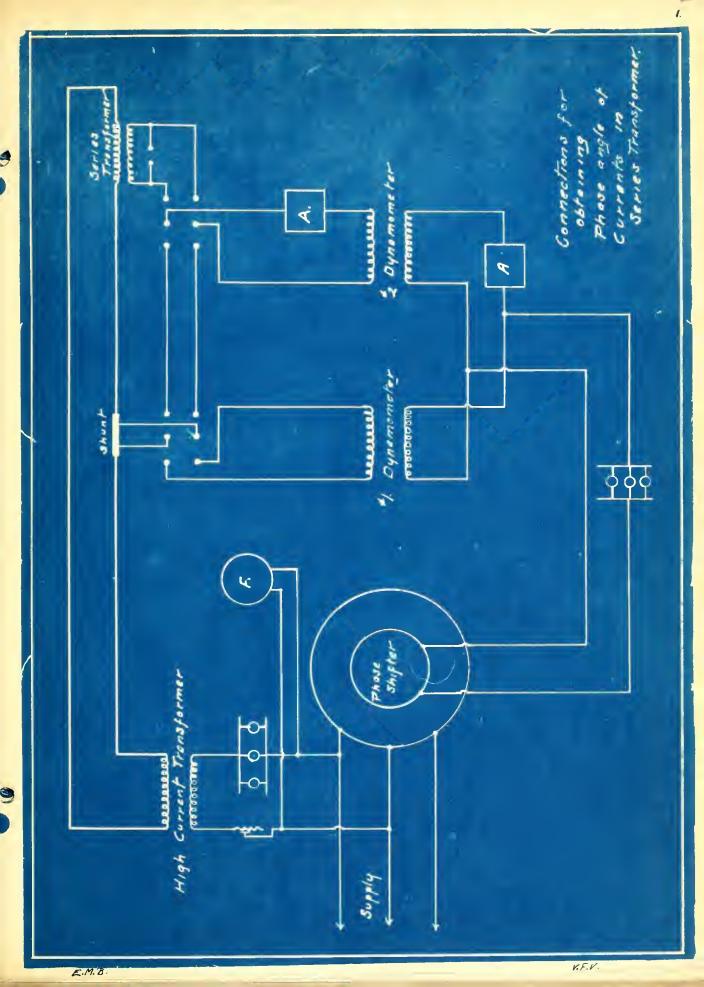
after a study of the curves and the data.

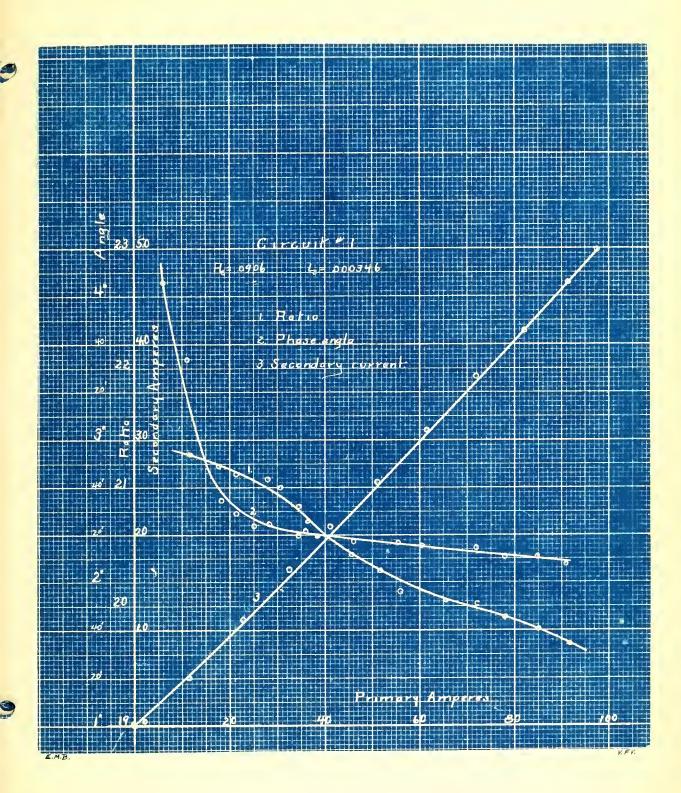
It will be noted that at about the usual operating power factor at light loads, the error due to the phase difference of the carrent and e.m.f. in the secondary often exceeds that due to the ratio, while at normal operations loads it is equal to or slightly greater then the ratio error. For full loads the angle error is usually smaller than the ratio error, and for power factors of 100% or nearly so, the angle error can be neglescied. Since the usual operating power factor is often much below 100%, the error due to the phase angle should also be considered in connection with that due to the ratio.

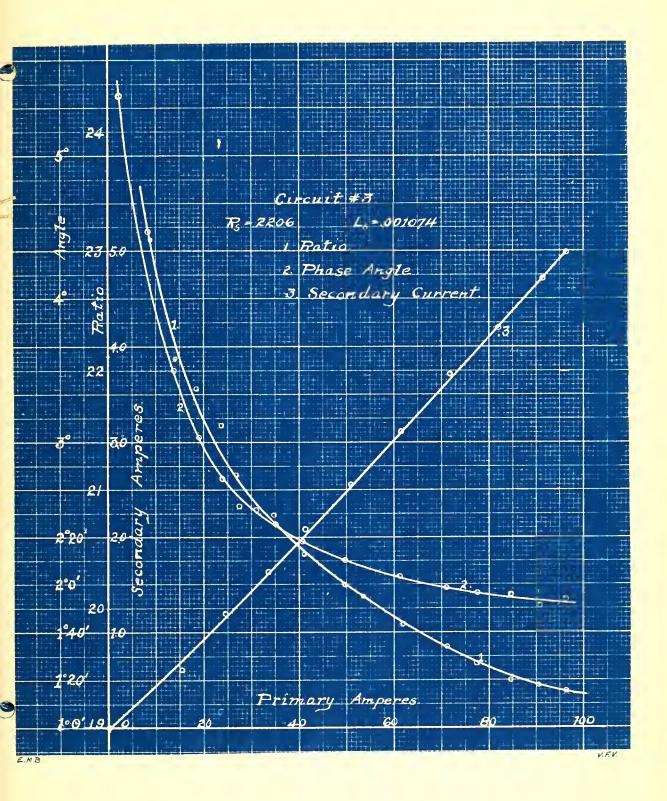




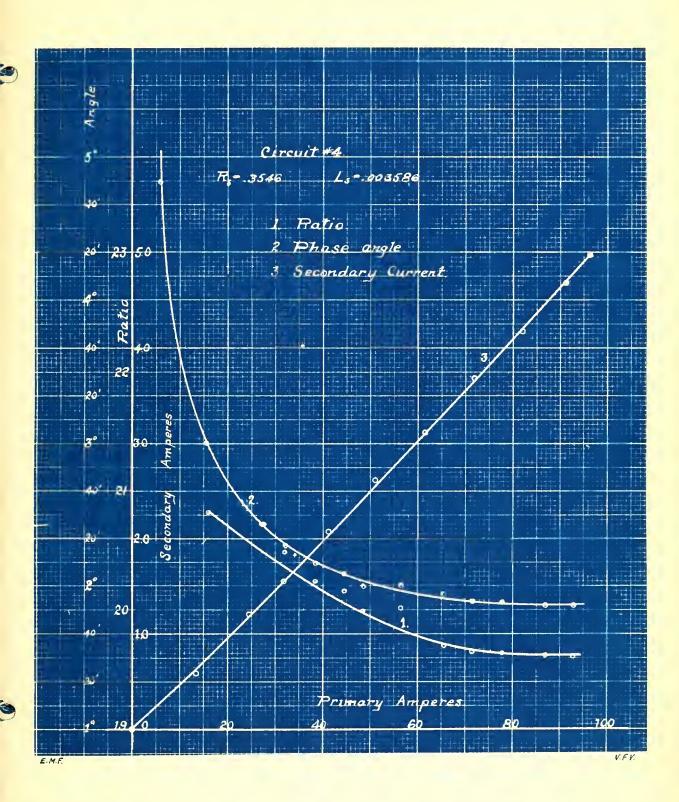


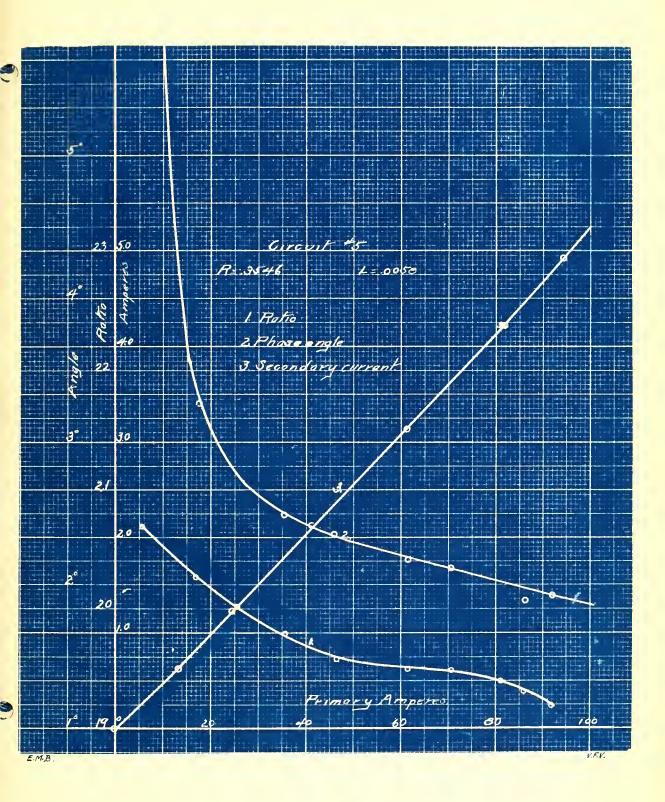




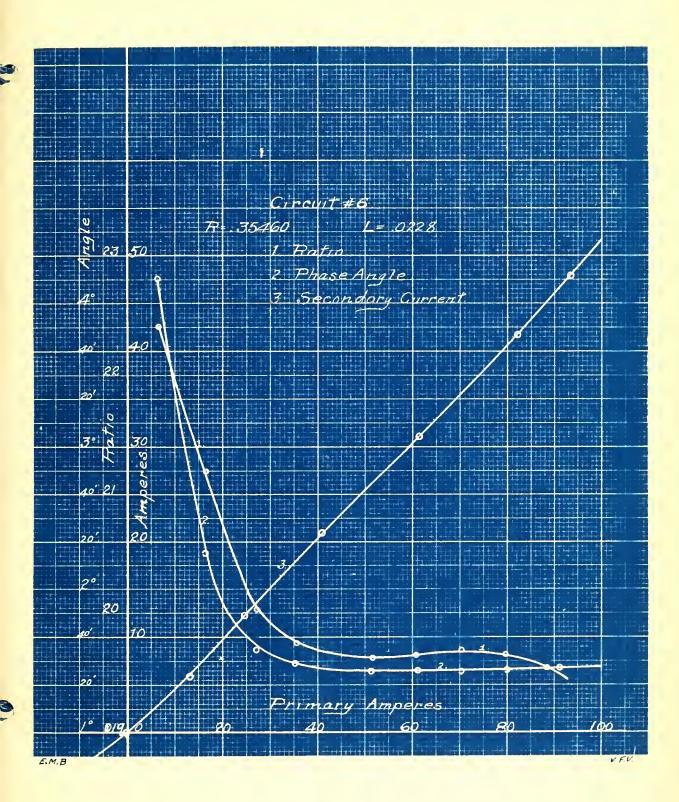


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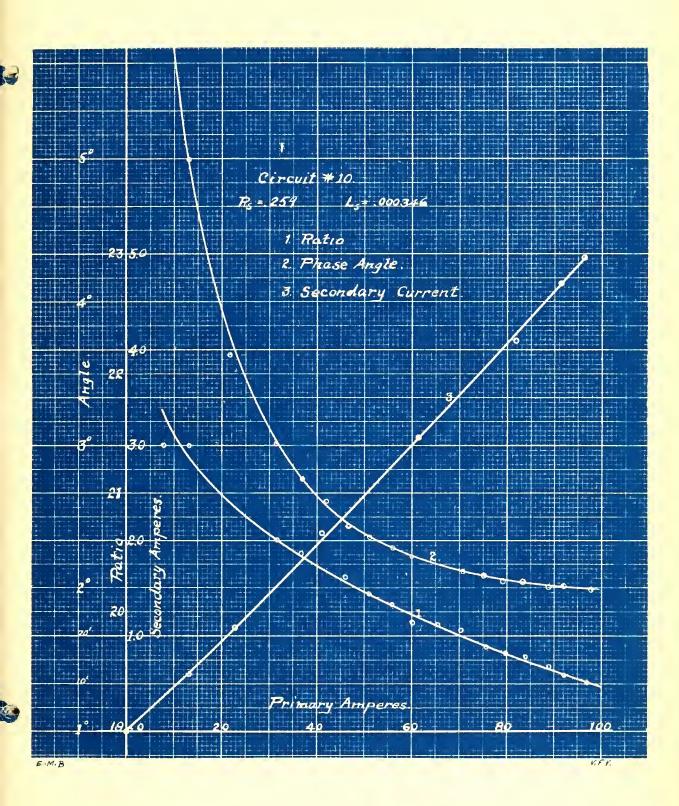


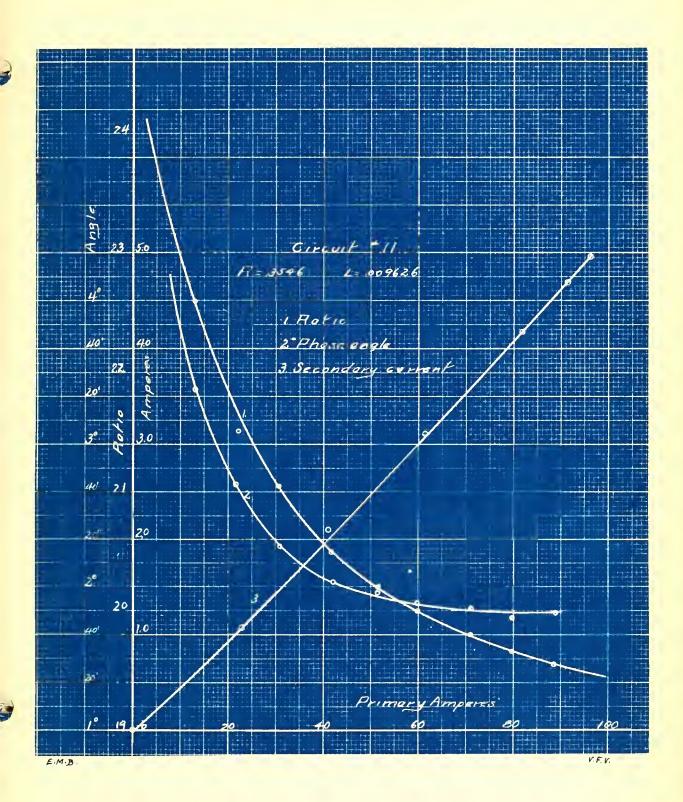
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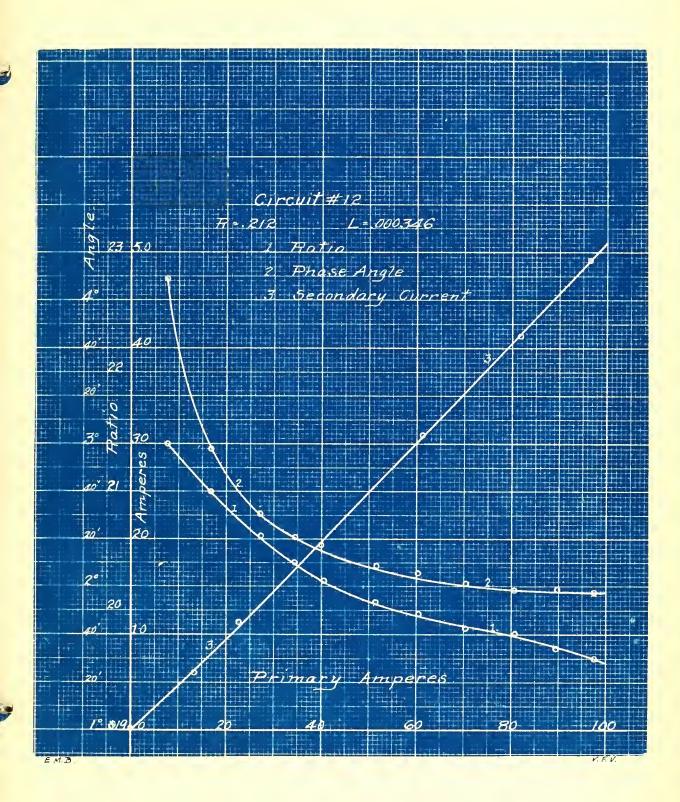
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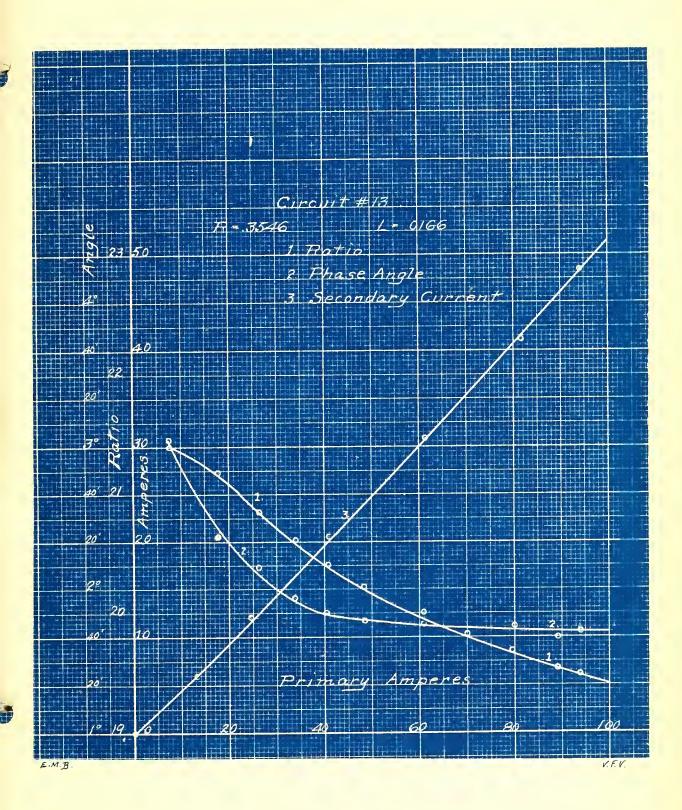


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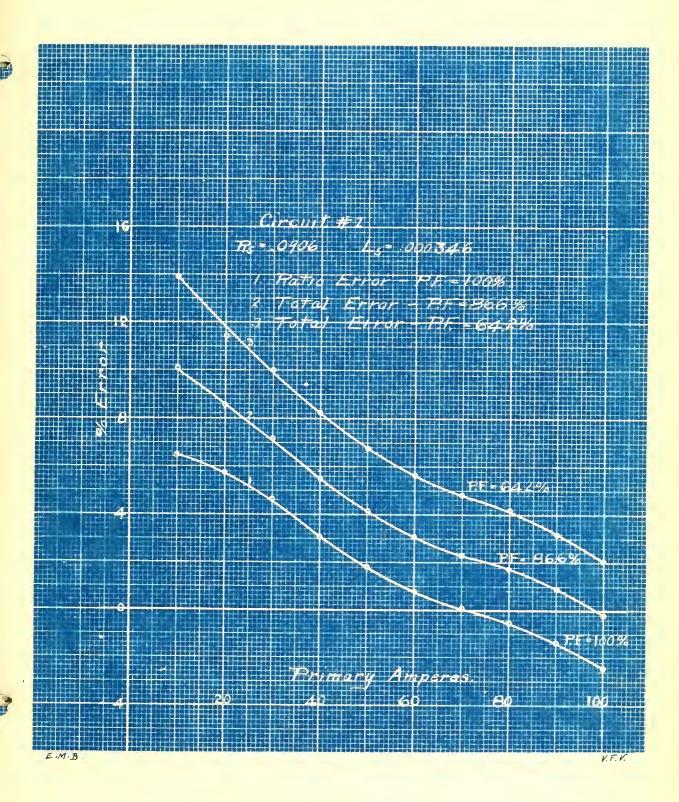
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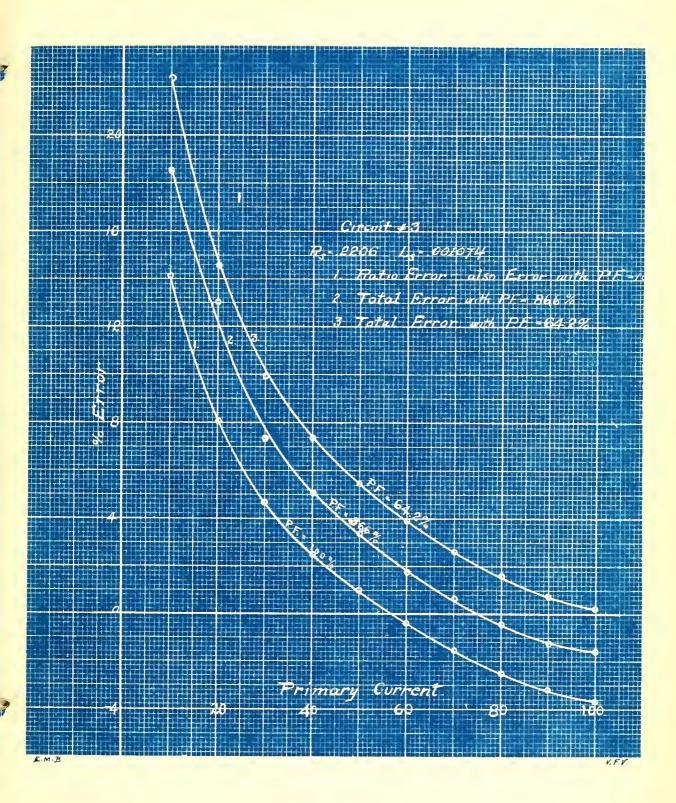
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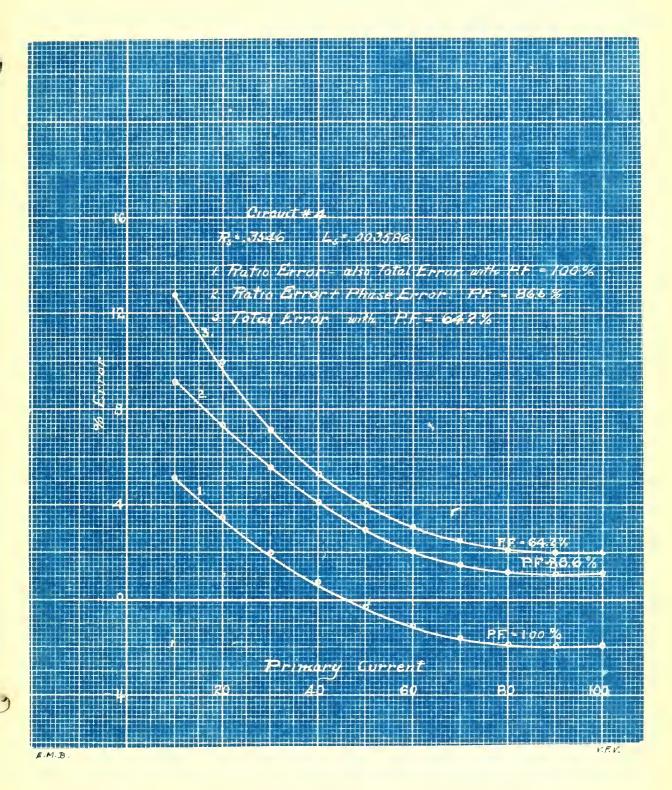
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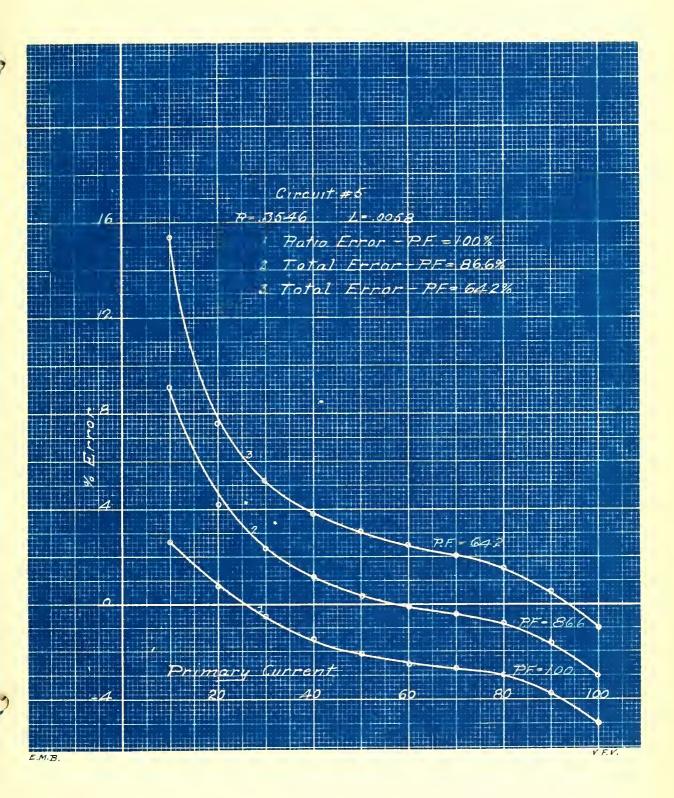
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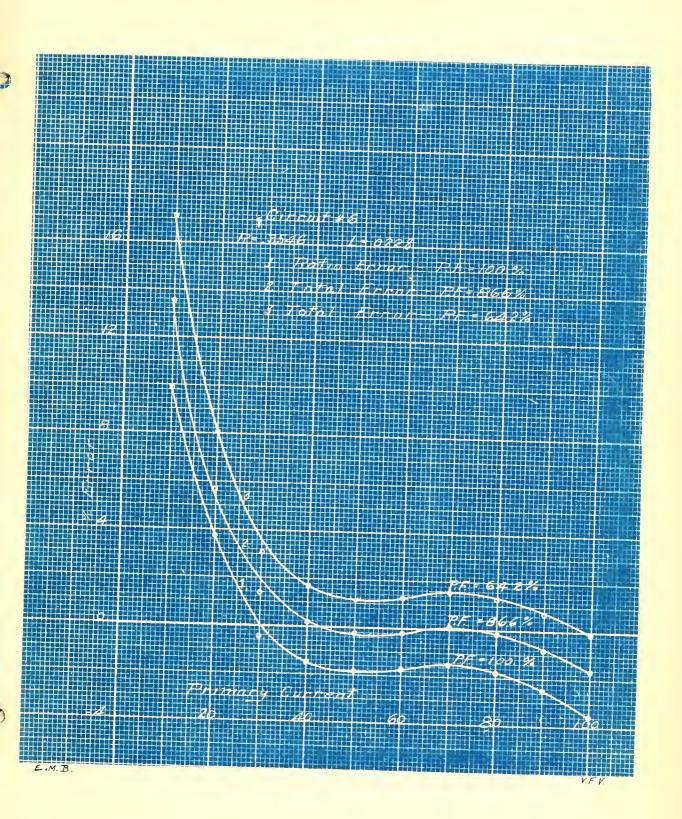
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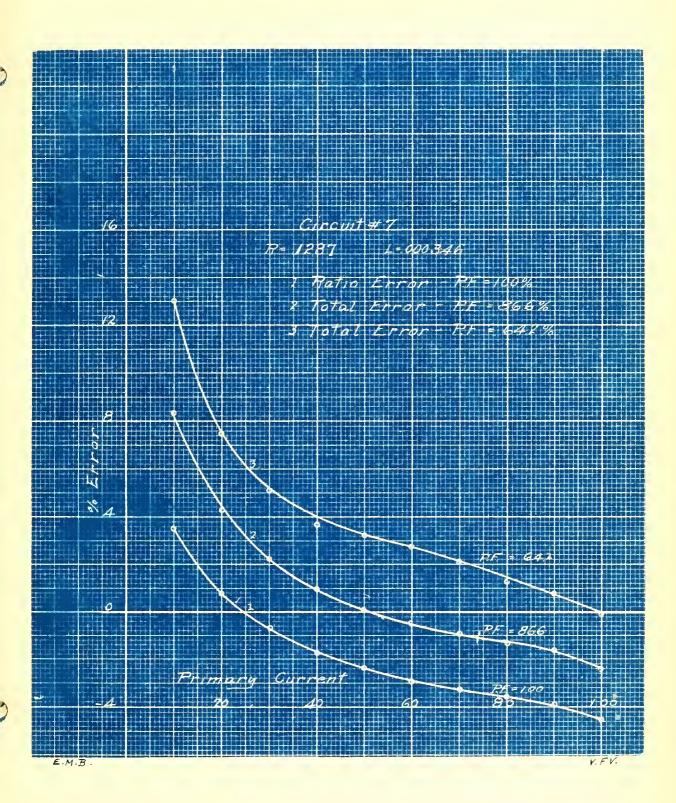
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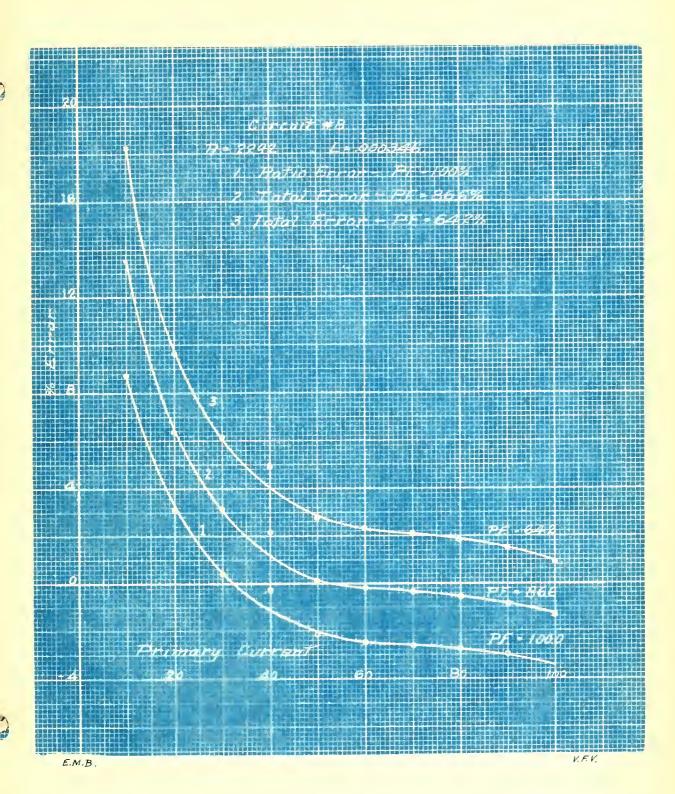
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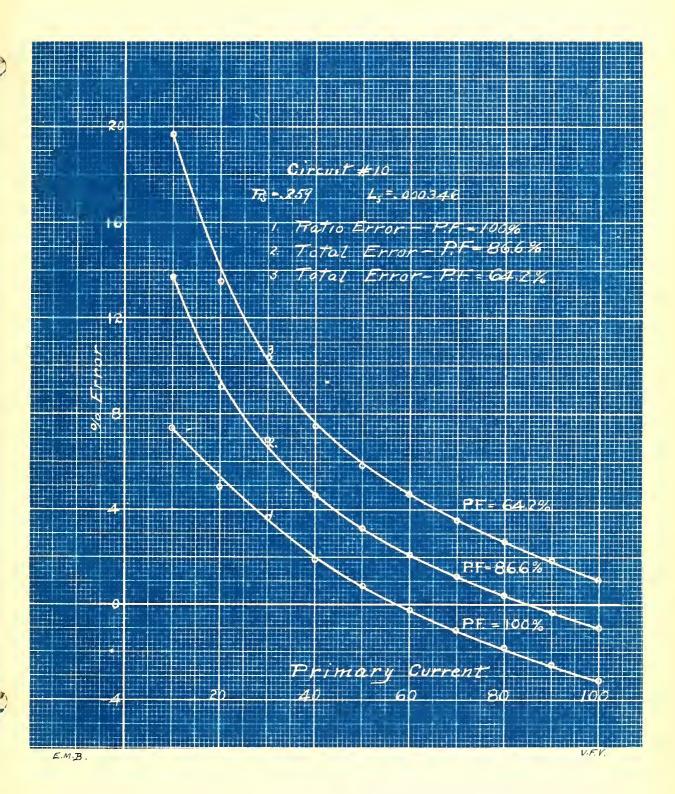
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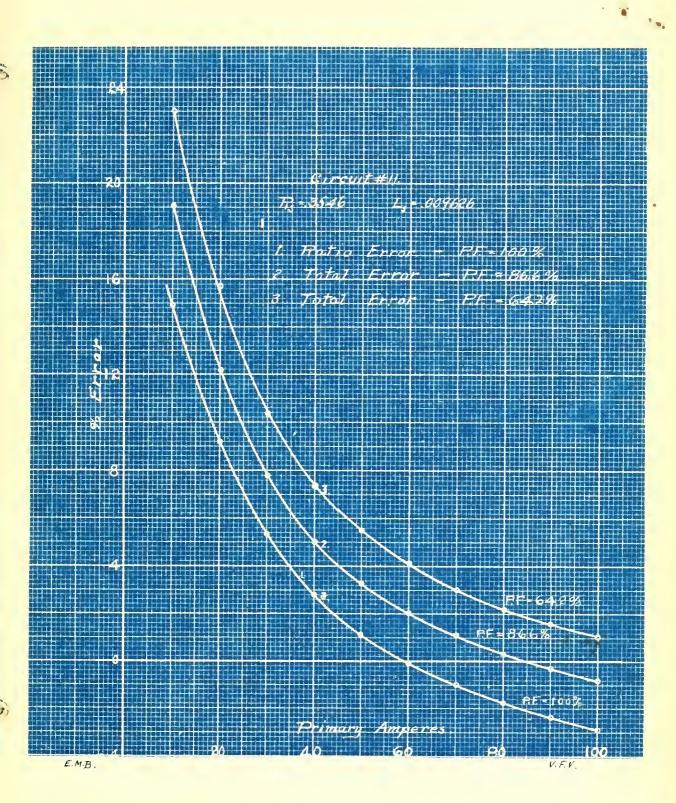
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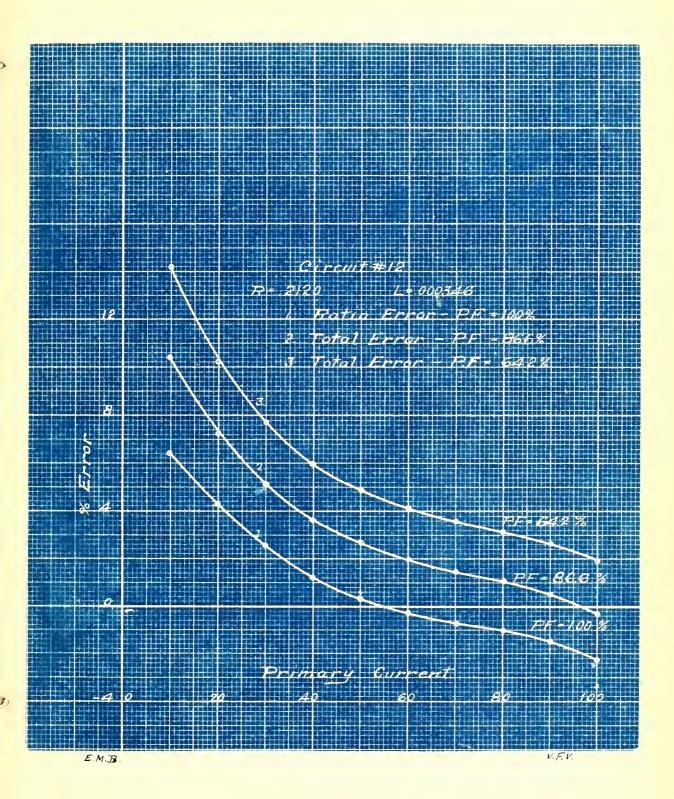
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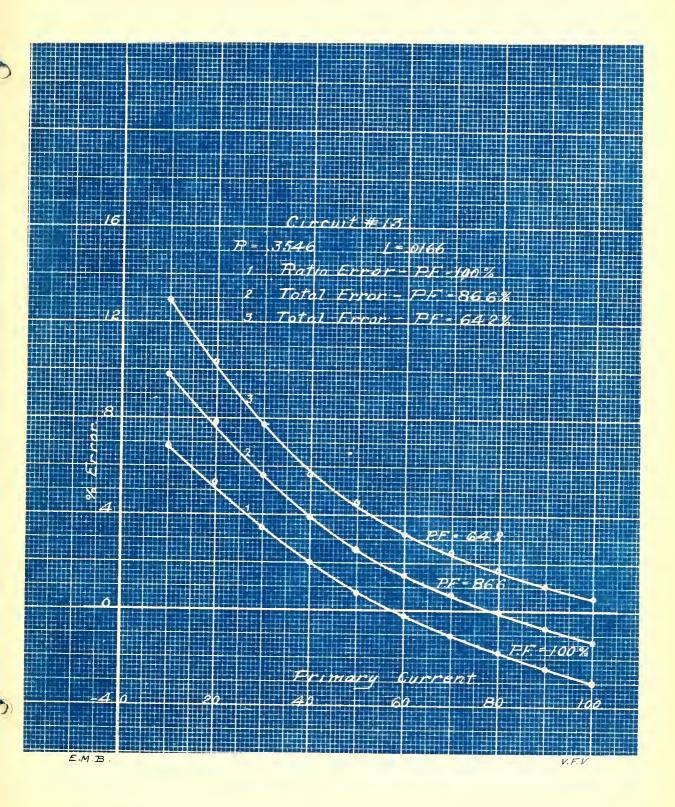
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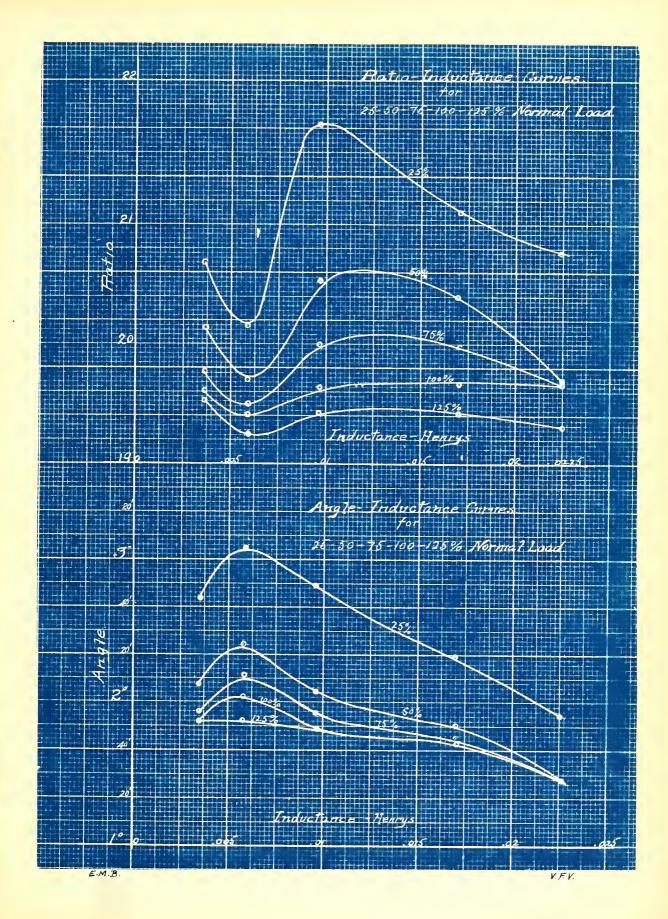


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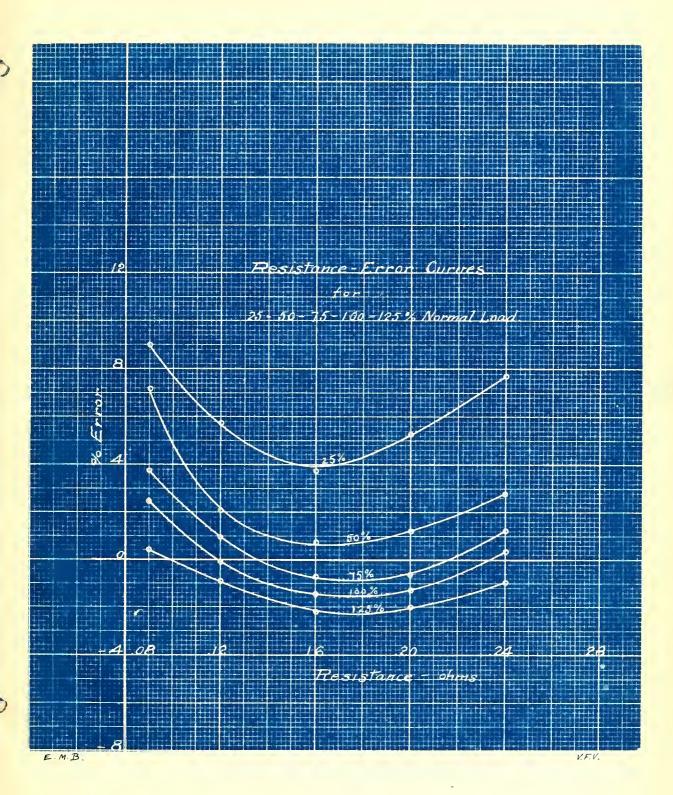


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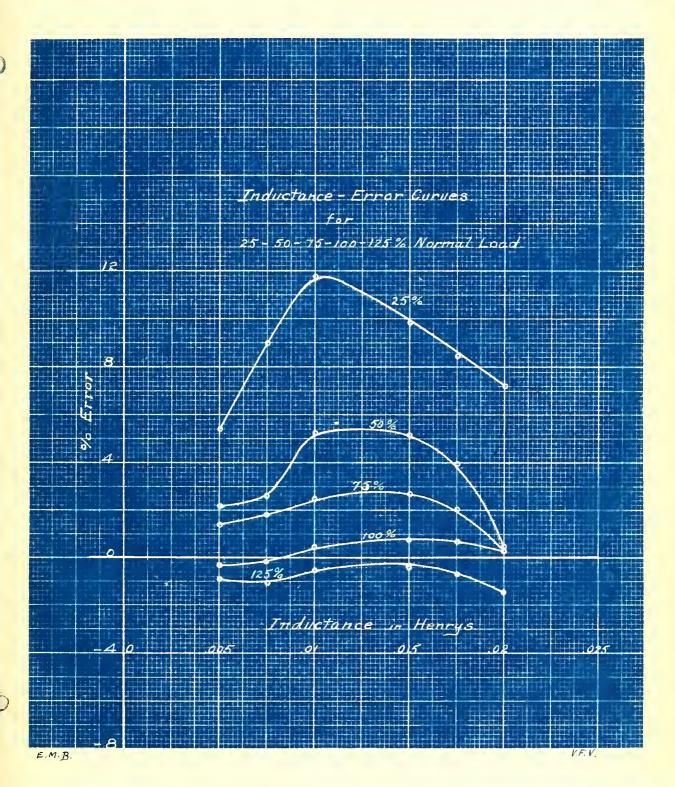
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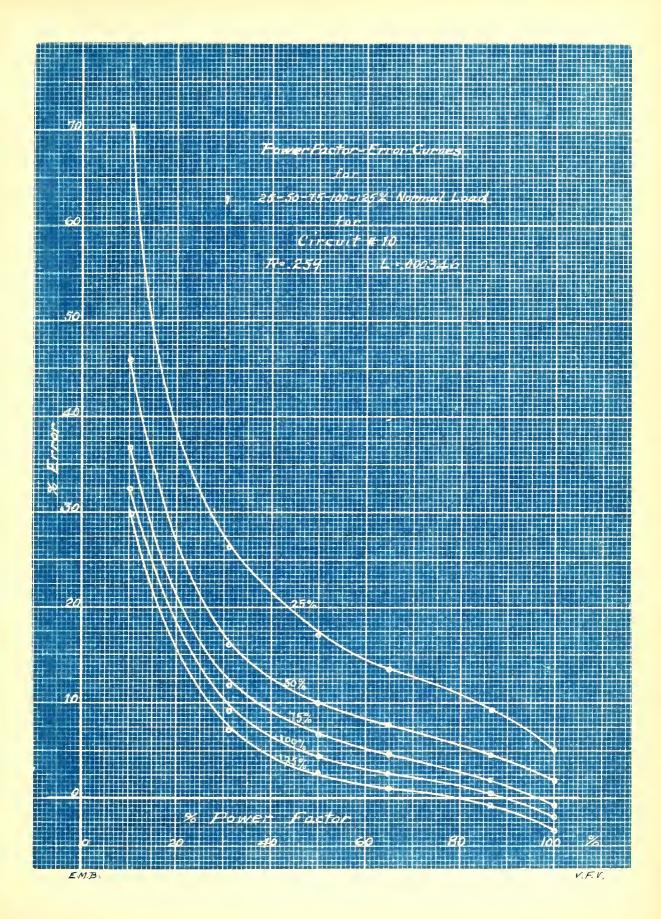


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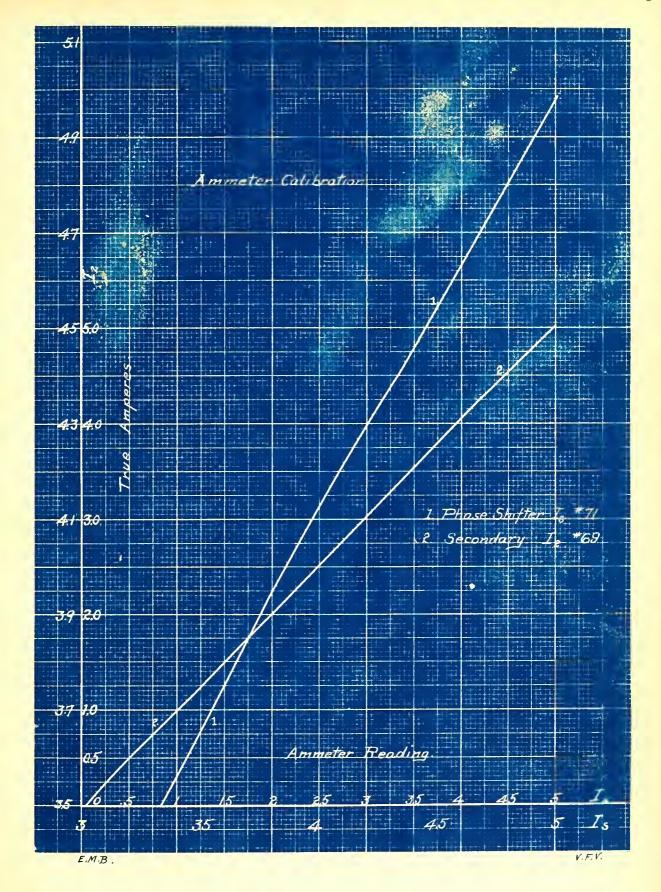
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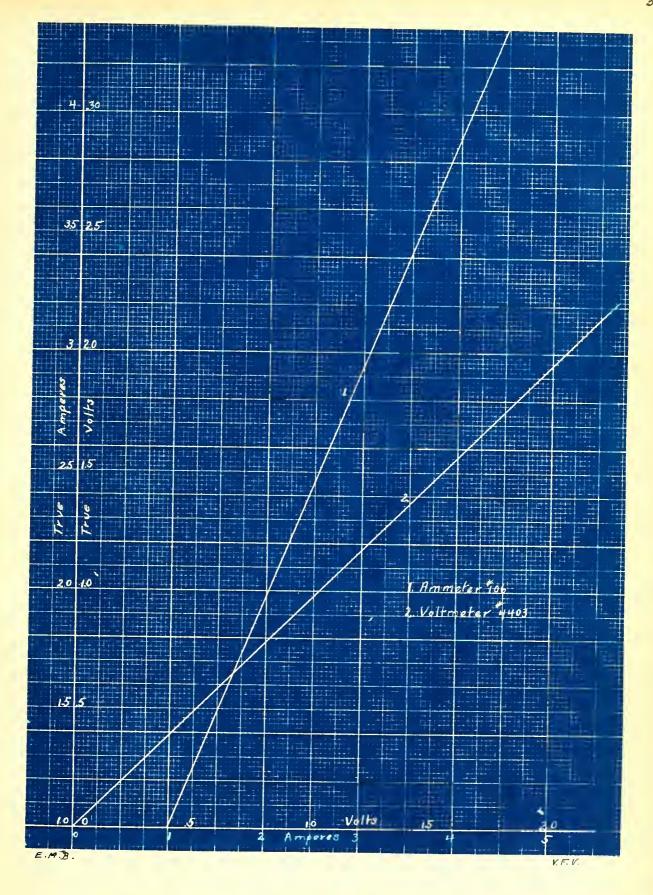
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